Middle East Technical University Department of Electrical and Electronics Engineering

EE 531 - HW #4

Due: Jan. 12, 2015

(to be collected before final exam)

- **1.** (Textbook) Exercise 4.8
- 2. (Textbook) Exercise 4.9
- 3. (Textbook) Exercise 4.10
- 4. (Textbook) Exercise 4.12
- 5. (Textbook) Exercise 4.15 (Feel free to have a look at your EE501 notes!)
- 6. (Textbook) Exercise 4.26
- 7. (Çınlar, Intro. Stoch. Processes, Problem 8.17) Consider two gamblers whose capitals sum to 7 dollars, so that as soon as one has seven dollars the other is ruined and the game stops. Plays form independent trials with even chances for winning and losing. Let X_n be the capital of the first gambler at the end of the *n*th play.
 - a) Show that X is a Markov chain with the state-space $E = \{0,...,7\}$ and transition probabilities $P_{i,i-1} = P_{i,i+1} = 1/2$ for $i = \{1,...,6\}$ and $P_{00} = P_{77} = 1$.
 - b) Compute the probability F_{i0} of eventual ruin for the first player for each possible initial capital *i*.
 - c) Assume first player starts with 6 dollars. Compute the probability that he loses 5 dollars during the game, i.e. comes to the brink of a total loss; but ends up bankrupting the other player, i.e. eventually reaching the state i = 7. (Hint: To calculate

 $F_{61} = P$ {ever reaching 1| starting at 6}, you may convert state 1 to an absorbing state.)