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CHAPTER I

From Biological to Artificial Neuron Model

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CHAPTER I : *From Biological to Artificial Neuron Model*

What

you

see

in

the

picture?

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- Is there any conventional computer at present with the capability of perceiving both the trees and Baker's transparent head in this picture at the same time?

- Most probably, the answer is no.

- Although such a visual perception is an easy task for human being, we are faced with difficulties when sequential computers are to be programmed to perform visual operations.

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Conventional Computers

- In a conventional computer, usually there exist a single processor implementing a sequence of arithmetic and logical operations, nowadays at speeds approaching 10^9 operations per second.

- However this type of devices have ability neither to adapt their structure nor to learn in the way that human being does.

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What traditional computers can't do?

- There is a large number of tasks for which it is proved to be virtually impossible to device an algorithm or sequence of arithmetic and/or logical operations.

- For example, in spite of many attempts, a machine has not yet been produced which will automatically read handwritten characters, or recognize words spoken by any speaker let alone translate from one language to another, or drive a car, or walk and run as an animal or human being [Hecht-Nielsen 88]

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Computers versus Brain

- What makes such a difference brain an conventional computers seems to be neither because of the processing speed of the computers nor because of their processing ability.

  - Today's processors have a speed 10^5 times faster than the basic processing elements of the brain called *neuron*.
  - When the abilities are compared, the neurons are much simpler.

- The difference is mainly due to the structural and operational trend.
  - While in a conventional computer the instructions are executed sequentially in a complicated and fast processor, the brain is a massively parallel interconnection of relatively simple and slow processing elements.

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1.1. Biological Neuron Human nervous system

- It is claimed that the human central nervous system is comprised of about $1,3x10^{10}$ neurons and that about $1x10^{10}$ of them takes place in the brain.

- At any time, some of these neurons are firing and the power dissipation due this electrical activity is estimated to be in the order of 10 watts.

- Monitoring the activity in the brain has shown that, even when asleep, $5x10^7$ nerve impulses per second are being relayed back and forth between the brain and other parts of the body. This rate is increased significantly when awake [Fischer 1987].

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1.1. Biological Neuron Neuron

- A neuron has a roughly spherical cell body called soma (Figure 1.1).
- The signals generated in soma are transmitted to other neurons through an extension on the cell body called *axon* or *nerve fibres*.
- Another kind of extensions around the cell body like bushy tree is the *dendrites*, which are responsible from receiving the incoming signals generated by other neurons. [Noakes 92]
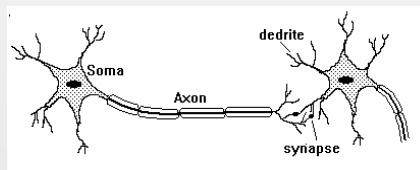

Figure 1.1. Typical Neuron

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1.1. Biological Neuron Axon

- An axon (Figure 1.2), having a length varying from a fraction of a millimeter to a meter in human body, prolongs from the cell body at the point called **axon hillock**.
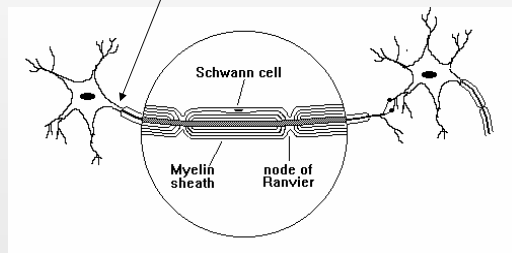

Figure 1.2. Axon

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1.1. Biological Neuron Synapses

- At the other end, the axon is separated into several branches, at the very end of which the axon enlarges and forms terminal **buttons**.
- Terminal buttons are placed in special structures called the **synapses** which are the junctions transmitting signals from one neuron to another (Figure 1.3).
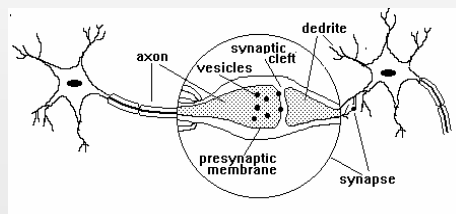

Figure 1.3. The synapse

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1.1. Biological Neuron Synapses

- A neuron typically drive 10^3 to 10^4 synaptic junctions
- The *synaptic vesicles* holding several thousands of molecules of chemical transmitters, take place in terminal buttons.
- When a nerve impulse arrives at the synapse, some of these chemical transmitters are discharged into synaptic *cleft*, which is the narrow gap between the terminal button of the neuron transmitting the signal and the membrane of the neuron receiving it.
- In general the synapses take place between an axon branch of a neuron and the dendrite of another one. Although it is not very common, synapses may also take place between two axons or two dendrites of different cells or between an axon and a cell body.

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1.1. Biological Neuron Ion pumps

- Neurons are covered with a semi-permeable membrane, with only 5 nanometer thickness.
- The membrane is able to selectively absorb and reject ions in the intracellular fluid. The membrane basically acts as an ion pump to maintain a different ion concentration between the intracellular fluid and extracellular fluid.
- While the sodium ions are continually removed from the intracellular fluid to extracellular fluid, the potassium ions are absorbed from the extracellular fluid in order to maintain an equilibrium condition.

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1.1. Biological Neuron *Resting Potential*

- Due to the difference in the ion concentrations inside and outside, the cell membrane become polarized.
- In equilibrium the interior of the cell is observed to be 70 milivolts negative with respect to the outside of the cell. The mentioned potential is called the ***resting potential***.

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1.1. Biological Neuron *graded potential*

- A neuron receives inputs from a large number of neurons via its synaptic connections. Nerve signals arriving at the presynaptic cell membrane cause chemical transmitters to be released in to the synaptic cleft.
- These chemical transmitters ***diffuse*** across the gap and join to the postsynaptic membrane of the receptor site. The membrane of the post-synaptic cell gathers the chemical transmitters.
- This causes either a decrease or an increase in the efficiency of the local sodium and potassium pumps depending on the type of the chemicals released in to the synaptic cleft.
- In turn, the soma potential, which is called ***graded potential***, changes.

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1.1. Biological Neuron Excitatory, Inhibitory synapses

- While the synapses whose activation decreases the efficiency of the pumps cause depolarization of the graded potential, the effects of the synapses that increase the efficiency of pumps result in hyperpolarization.
- The first kind of synapses encouraging depolarization is called *excitatory* and the others discouraging it are called *inhibitory* synapses.

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1.1. Biological Neuron Firing

- If the decrease in the neuron polarization is adequate to exceed a threshold then the post-synaptic neuron *fires*.
- The arrival of impulses to excitatory synapses adds to the depolarization of soma while inhibitory effect tends to cancel out the depolarizing effect of excitatory impulse.
- In general, although the depolarization due to a single synapse is not enough to fire the neuron, if some other areas of the membrane are depolarized at the same time by the arrival of nerve impulses through other synapses, it may be adequate to exceed the threshold and fire.

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CHAPTER I : *From Biological to Artificial Neuron Model*

1.1. Biological Neuron Action Potential

- At the axon hillock, the excitatory effects result in the interruption the regular ion transportation through the cell membrane, so that the ionic   concentrations immediately begin to equalize as ions diffuse through the membrane.
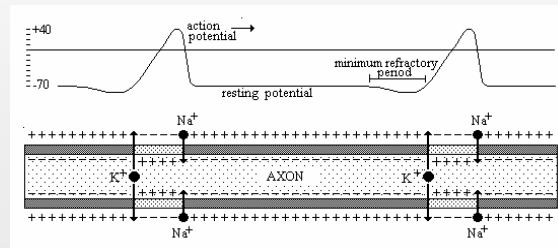

Figure 1.4. The action potential on axon

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1.1. Biological Neuron Action Potential

- If the depolarization is large enough, the membrane potential at axon hillock eventually collapses, and for a short period of time the internal potential becomes positive.
- The *action potential* is the name of this brief reversal in the potential, which results in an electric current flowing from the region at action potential to an adjacent axon region with a resting potential.
- This current causes the potential of the next resting region to change, so the effect propagates in this manner along the axon membrane wall.
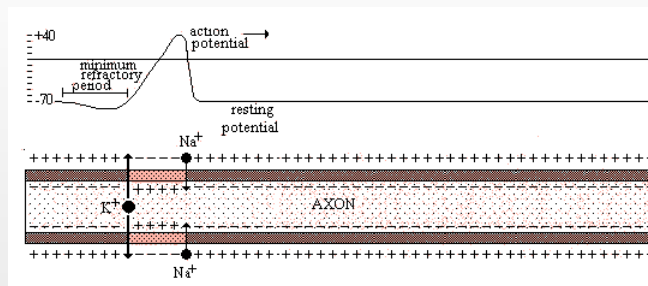
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CHAPTER I : *From Biological to Artificial Neuron Model*

1.1. Biological Neuron Refractory Period

- Once an action potential has passed a given point, it is incapable of being reexcited for a while called *refractory period.*
- Because the depolarized parts of the neuron are in a state of recovery and can not immediately become active again, the pulse of electrical activity always propagates in only forward direction.
- The previously triggered region then rapidly recovers to the polarized resting state due to the action of the sodium potassium pumps.
- The refractory period is about 1 milliseconds, and this limits the nerve pulse transmission so that a neuron can typically fire and generate nerve pulses at a rate up to 1000 pulses per second.

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1.1. Biological Neuron Propagation of signals on axon

- The number of impulses and the speed at which they arrive at the synaptic junctions to a particular neuron determine whether the total excitatory depolarization is sufficient to cause the neuron to fire and so to send a nerve impulse down its axon.
- The depolarization effect can propagate along the cell wall but these effects can be dissipated before reaching the axon.
- However, once the nerve impulse created at axon hillock it will propagate in axon   until it reaches the synapses where the depolarization effect will cause the release of chemical transmitters into the synaptic cleft.

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1.1. Biological Neuron pulses on axon

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1.1. Biological Neuron Myelin sheath and nodes of Ranvier

- The axons are generally enclosed by *myelin sheath* that is made of many layers of Schwann cells promoting the growth of the axon.
- The speed of propagation down the axon depends on the thickness of the myelin sheath that provides for the insulation of the axon from the extracellular fluid and prevents the transmission of ions across the membrane.
- The myelin sheath is interrupted at regular intervals by narrow gaps called *nodes of Ranvier* where extracellular fluid makes contact with membrane and the transfer of ions occur.

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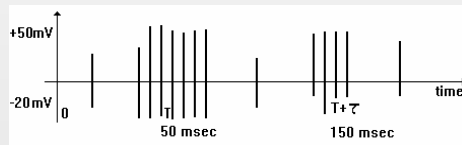#### *1.1. Biological Neuron Myelin sheath and nodes of Ranvier*

- Since the myelin sheath is poor conductor, the action potential is transmitted as depolarizations occur at the nodes of Ranvier.
- This happens in a sequential manner so that the depolarization of a node triggers the depolarization of the next one.
- The nerve impulse effectively jumps from a node to the next one along the axon each node acting rather like a regeneration amplifier to compensate for losses.
- Once an action potential is created at the axon hillock, it is transmitted through the axon to other neurons.

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CHAPTER I : *From Biological to Artificial Neuron Model*

1.1. Biological Neuron The nature of signal transmission in the ns

- It is mostly tempted to conclude the signal transmission in the nervous system as having a digital nature in which a neuron is assumed to be either fully active or inactive.
- However this conclusion is not that correct, because the intensity of a neuron signal is coded in the frequency of pulses.
- A better conclusion would be to interpret the biological neural systems as if using a form of pulse frequency modulation to transmit information.

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CHAPTER I : *From Biological to Artificial Neuron Model*

1.1. Biological Neuron The nature of signal transmission in the ns

- The nerve pulses passing along the axon of a particular neuron are of approximately constant amplitude but the number generated pulses and their time spacing is controlled by the statistics associated with the arrival at the neuron's many synaptic junctions of sufficient excitatory inputs [Müller and Reinhardt 90].
- The representation of biophysical neuron output behavior is shown schematically in Figure 1.5. [Kandel 85, Sejnowski 81]

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CHAPTER I : *From Biological to Artificial Neuron Model*

1.1. Biological Neuron The nature of signal transmission in the ns

- At time t=0 a neuron is excited; at time T, typically it may be of the order of 50 milliseconds, the neuron fires a train of impulses along its axon. Each of these impulses is practically of identical amplitude.
- Some time later, say around t=T+τ, the neuron may fire another train of impulses, as a result of the same excitation, though the second train of impulses will usually contain a smaller number. Even when the neuron is not excited, it may send out impulses at random, though much less frequently than the case when it is excited.
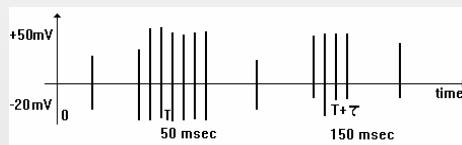

Figure 1.5. Representation of biophysical neuron output signal after excitation at tine t=0

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1.2. Artificial Neuron Model

- As it is mentioned in the previous section, the transmission of a signal from one neuron to another through synapses is a complex chemical process in which specific transmitter substances are released from the sending side of the junction.
- The effect is to raise or lower the electrical potential inside the body of the receiving cell. If this potential reaches a threshold, the neuron fires.
- It is this characteristic that the artificial neuron model proposed by McCulloch and Pitts, [McCulloch and Pitts 1943] attempt to reproduce.

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CHAPTER I : *From Biological to Artificial Neuron Model*

1.2. Artificial Neuron Model

$$u_1 \xrightarrow{\quad} \boxed{w_1}$$
$$u_2 \xrightarrow{\quad} \boxed{w_2}$$
$$a = (\sum_{j=1}^{N} u_j w_j) + \theta \quad x = f(a) \quad x$$
$$u_j \xrightarrow{\quad} \boxed{w_j}$$
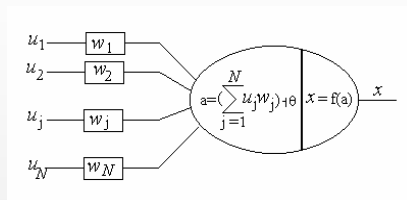$$u_N \xrightarrow{\quad} \boxed{w_N}$$

Figure 1.6. Artificial Neuron

- The neuron model shown in Figure 1.6 is the one that widely used in artificial neural networks with some minor modifications on it.
  - It has N input, denoted as $u_1, u_2, ...u_N$.
  - Each line connecting these inputs to the neuron is assigned a weight, which are denoted as $w_1, w_2, .., w_N$ respectively. Weights in the artificial model correspond to the synaptic connections in biological neurons.
  - θ represent *threshold* in artificial neuron.
  - The inputs and the weights are real values.

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CHAPTER I : *From Biological to Artificial Neuron Model*

1.2. Artificial Neuron Model Neuron Activation

🔹 The activation is given by the formula:

$$a = (\sum_{j=1}^{N} w_j u_j) + \theta$$

(1.2.1)

🔹 A negative value for a weight indicates an inhibitory connection while a positive value indicates an excitatory one.

🔹 Although in biological neurons, θ has a negative value, it may be assigned a positive value in artificial neuron models. If θ is positive, it is usually referred as ***bias***. For its mathematical convenience we will use (+) sign in the activation formula.

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1.2. Artificial Neuron Model Neuron Activation

🔹 Sometimes, the threshold is combined for simplicity into the summation part by assuming an imaginary input $u_0 = +1$ and a connection weight $w_0 = \theta$. Hence the activation formula becomes:

$$a = \sum_{j=0}^{N} w_j u_j$$

(1.2.2)

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1.2. Artificial Neuron Model *Neuron Activation*

■ The vector notation

$$a = \mathbf{w}^\mathsf{T}\mathbf{u} + \theta \qquad\qquad (1.2.3)$$

is useful for expressing the activation for a neuron.
■ Here, the jth element of the input vector $\mathbf{u}$ is u_j and the jth element of the weight vector of $\mathbf{w}$ is w_j. Both of these vectors are of size N.
■ Notice that, $\mathbf{w}^\mathsf{T}\mathbf{u}$ is the inner product of the vectors $\mathbf{w}$ and $\mathbf{u}$, resulting in a scalar value. The inner product is an operation defined on equal sized vectors. In the case these vectors have unit length, the inner product is a measure of similarity of these vectors.

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1.2. Artificial Neuron Model *Neuron output*

■ The output value of the neuron is a function of its activation in an analogy to the firing frequency of the biological neurons:

$$x = f(a) \qquad\qquad (1.2.4)$$

■ Originally the neuron output function $f(a)$ in McCulloch Pitts model proposed as threshold function, however linear, ramp and sigmoid functions (Figure 1.7.) are also widely used output functions.

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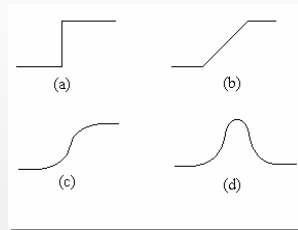
1.2. Artificial Neuron Model *Neuron output function*

Figure 1.7. Some neuron output functions;

a) threshold function
b)ramp function,
c) sigmoid function,
d)Gaussian function

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1.2. Artificial Neuron Model *Neuron output*

Linear: $f(a) = \kappa a$ (1.2.5)

Threshold: $f(a) = \begin{cases} 0 & a \le 0 \\ 1 & 0 < a \end{cases}$ (1.2.6)

Ramp: $f(a) = \begin{cases} 0 & a \le 0 \\ a/\kappa & 0 < a \le \kappa \\ 1 & \kappa < a \end{cases}$ (1.2.7)

Sigmoid: (1.2.8)

$$f(a) = \frac{1}{1 + e^{-\kappa a}}$$

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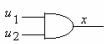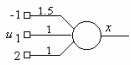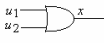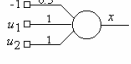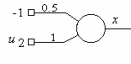#### 1.2. *Artificial Neuron Model Implementation of lf by an*

- Though its simple structure, McCulloch-Pitts neuron is a powerful computational device.
- McCulloch and Pitts proved that a synchronous assembly of such neurons is capable in principle to perform any computation that an ordinary digital computer can, though not necessarily so rapidly or conveniently [Hertz et al 91].

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1.2. *Artificial Neuron Model Example 1.1*

When the threshold function is used as the neuron output function, and binary input values 0 and 1 are assumed, the basic Boolean functions AND, OR and NOT of two variables can be implemented by choosing appropriate weights and threshold values, as shown in Figure 1.8.

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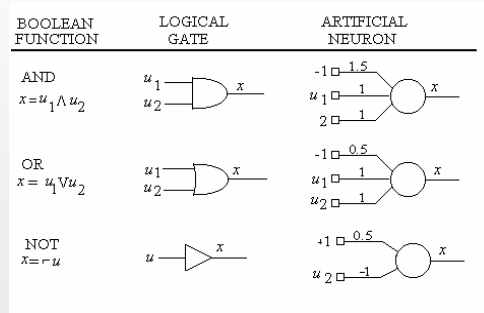
1.2. Artificial Neuron Model Example 1.1

Figure 1.8. Implementation of Boolean functions by artificial neuron

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1.3. Network of Neurons

- While a single artificial neuron is not be able to implement some boolean functions, the problem is overcome by connecting the outputs of some neurons as input to the others, so constituting a neural network.
- Suppose that we have connected many artificial neurons that we introduced in Section 1.2 to form a network. In such a case, there are several neurons in the system, so we assign indices to the neurons to discriminate between them.

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CHAPTER I : *From Biological to Artificial Neuron Model*

1.3. Network of Neurons

■ Then to express the activation or output of ith neuron, the formulas are modified as follows:

$$a_i = (\sum_{j=1}^{N} w_{ji} x_j) + \theta_i \qquad (1.3.1)$$

where x_j may be either the output of a neuron determined as

$$x_j = f_j(a_j) \qquad (1.3.2)$$

or an external input determined as:

$$x_j = u_j \qquad (1.3.3)$$

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CHAPTER I : *From Biological to Artificial Neuron Model*

1.3. Network of Neurons

■ In some applications the threshold value θi is determined by the external inputs.

■ Due to the equation (1.3.1) sometimes it may be convenient to think all the inputs are connected to the network only through the threshold of some special neurons called the input neurons. They are just conveying the input value connected to their threshold as $\theta j = u j$ to their output xj with a linear output transfer function $fj(a)=a$.

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CHAPTER I : *From Biological to Artificial Neuron Model*

1.3. Network of Neurons

- For a neural network we can define a state vector $\mathbf{x}$ in which the ith component is the output of ith neuron, that is x_i.

- Furthermore we define a weight matrix $\mathbf{W}$, in which the component w_{ji} is the weight of the connection from neuron j to neuron i.

- Therefore we can represent the system as:

$$\mathbf{x} = \mathbf{f}(\mathbf{W}^{\mathsf{T}}\mathbf{x} + \theta) \tag{1.3.4}$$

Here θ is the vector whose i^{th} component is θ_i and $\mathbf{f}$ is used to denote the vector function such that the function $\mathbf{f}_i$ is applied at the ith component of the vector.

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CHAPTER I : *From Biological to Artificial Neuron Model*

1.3. Network of Neurons

Example 1.2: A simple example often given to illustrate the behavior of a neural networks is the one used to implement the XOR (exclusive OR) function. Notice that it is not possible to obtain exclusive-or or equivalence function, by using a single neuron. However this function can be obtained when outputs of some neurons are connected as inputs to some other neurons. Such a function can be obtained in several ways, only two of them being shown in Figure 1.9.
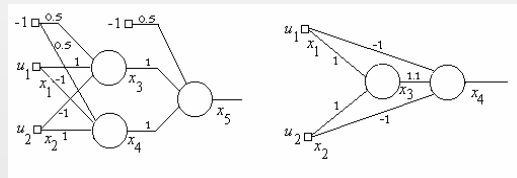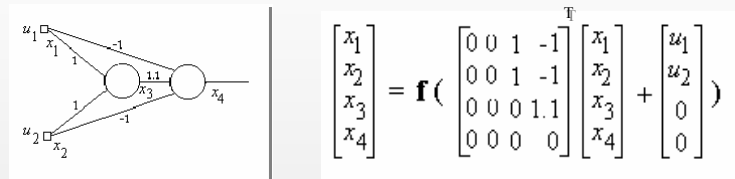

Figure 1.9. Various implementations of the exclusive-or function by using artificial neuron

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CHAPTER I : *From Biological to Artificial Neuron Model*

1.3. Network of Neurons

The second neural network of Figure 1.9 can be represented as:

$$
\begin{bmatrix} x_1 \\ x_2 \\ x_3 \\ x_4 \end{bmatrix} = \mathbf{f}\left(\begin{bmatrix} 0 & 0 & 1 & -1 \\ 0 & 0 & 1 & -1 \\ 0 & 0 & 0 & 1.1 \\ 0 & 0 & 0 & 0 \end{bmatrix}^{\mathrm{T}} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \\ x_4 \end{bmatrix} + \begin{bmatrix} u_1 \\ u_2 \\ 0 \\ 0 \end{bmatrix} \right)
$$

where f_1 and f_2 being linear identity function, f_3 and f_4 being threshold functions.

In the case of binary input, $u_i \in \{0,1\}$ or bipolar input, that is $u_j \in \{-1,1\}$, all of f_i may be chosen as threshold function.
The diagonal entries of the weight matrix are zero, since the neurons do not have self-feedback in this example.
The weight matrix is upper triangular, since the network is feedforward.

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1.4. Network Architectures

- Neural computing is an alternative to programmed computing which is a mathematical model inspired by biological models.
- This computing system is made up of a number of artificial neurons and a huge number of interconnections between them.
- According to the structure of the connections, we identify different classes of network architectures (Figure 1.10).
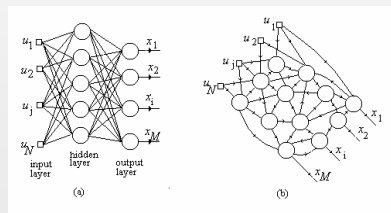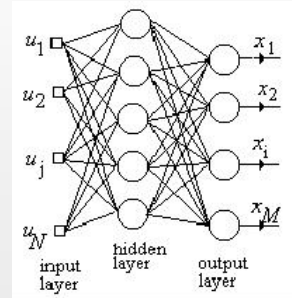
Figure 1.10 a) layered feedforward neural network
b) nonlayered recurrent neural network

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1.4. Network Architectures Feedforward Neural networks

- In *feedforward* neural networks, the neurons are organized in the form of layers.
- The neurons in a layer get input from the previous layer and feed their output to the next layer. In this kind of networks connections to the neurons in the same or previous layers are not permitted.
- The last layer of neurons is called the *output layer* and the layers between the input and output layers are called the *hidden layers*.
- The *input layer* is made up of special input neurons, transmitting only the applied external input to their outputs.

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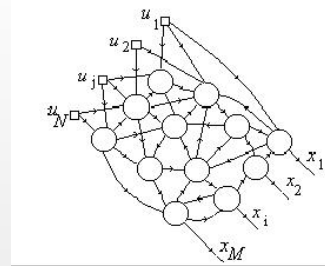CHAPTER I : *From Biological to Artificial Neuron Model*

1.4. Network Architectures Feedforward Neural networks

- In a network, if there is only the layer of input   nodes and a single layer of neurons   constituting the output layer then they   are called *single layer* network.
- If there are one or more hidden layers, such   networks   are   called *multilayer networks*.
- For a feed-forward network always exists an   assignment of indices to neurons resulting in a triangular weight matrix.   Furthermore   if the diagonal entries are zero this indicates that there is no self-feedback on the neurons.

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1.4. Network Architectures Recurrent Neural Networks

■ The structures, in which connections to the neurons of the same layer or   to the previous layers are allowed, are called *recurrent* networks.

■ In recurrent networks, due to feedback, it is not possible to obtain a   triangular weight matrix with any assignment of the indices.

thank you

Uğur HALICI