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> # Prof. Dr. Serkan Dağ
> # ME 310 Numerical Methods
> # File 13.4
> # Euler's Method
> # Solves the system of ODEs  $dy_1/dt=f_1$ ,  $dy_2/dt=f_2, \dots$ ,  $dy_n/dt=f_n$ 
> # Applicable for both linear and nonlinear ODE's
> # Interval of interest is [a,b]
> # n is the number of segments

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> restart :
> Digits := 16 :

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> # Open the output file

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> out := fopen("E:\\Courses\\2019_Spring\\ME310\\Files\\result.txt", 'WRITE', 'TEXT') :

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> # Define the right-hand-side functions

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> f1 := v;
> f2 := - ( c / m ) · v - ( k / m ) · x;

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$$f1 := v$$

$$f2 := -\frac{c v}{m} - \frac{k x}{m}$$

(1)

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> # Define the parameters

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> m := 20 :
> c := 5 :
> k := 20 :

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> # Interval end points

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> a := 0. :
> b := 15. :

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> # Number of segments

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> n := 64 :

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> # Initial conditions

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> x0 := 1 :
> v0 := 0 :

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> # Step size

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> h := (b - a) / n;

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$$h := 0.2343750000000000$$

(2)

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> # Analytical solution

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> omega := (3 · sqrt(7)) / 8 :

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> A := 1 :

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> B := 0.125 / omega :

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> xtrue := exp(- t / 8) · (A · cos(omega · t) + B · sin(omega · t)) :

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> vtrue := diff(xtrue, t) :

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> # Initiate the integration

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> t0 := a :

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> for i from 1 by 1 to n
>   while true do

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if $i = 1$ then

#printf("n %5.1f%10.5f%15.8f%15.8f%15.8f%15.8f", $i - 1$, t_0 , x_0 , v_0 , x_0 , v_0) :
fprintf(*out*, "n %5.1f%10.5f%15.8f%15.8f%15.8f%15.8f", $i - 1$, t_0 , x_0 , v_0 , x_0 , v_0) :

end if:

$x := x_0 + \text{subs}(\{v = v_0\}, f_1) \cdot h :$

$v := v_0 + \text{subs}(\{v = v_0, x = x_0\}, f_2) \cdot h :$

$tn := t_0 + h :$

$x_{truen} := \text{subs}(t = tn, x_{true}) :$

$v_{truen} := \text{subs}(t = tn, v_{true}) :$

#printf("n %5.1f%10.5f%15.8f%15.8f%15.8f%15.8f", i , tn , x_{truen} , v_{truen} , x , v) :
fprintf(*out*, "n %5.1f%10.5f%15.8f%15.8f%15.8f%15.8f", i , tn , x_{truen} , v_{truen} , x , v) :

$t_0 := tn :$

$x_0 := x :$

$v_0 := v :$

end do:

[
> *fclose*(*out*) :
[
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