

## Title: Byproducts: exotic $\mathbb{R}^4$ 's

Once Donaldson's exclusion appeared, it became clear that there must be exotic  $\mathbb{R}^4$ 's which are the smooth 4-manifolds homeomorphic but not diffeomorphic to  $\mathbb{R}^4$ . The talk will be started with construction of non-smoothable  $P_{E_8}$ -manifold, which has a historical importance in famous Poincare's conjecture, besides being a key in constructing our exotic manifolds. Afterwards uncountably many exotic  $\mathbb{R}^4$ 's will be constructed and it will be proved that they all have different smooth structures. If time permits, h-cobordism theorem and its failure in the dimension 4 will be stated, which helps us to exhibit another types of (small) exotic  $\mathbb{R}^4$ .