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**Chapter 5**  
**Gases**

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## Warning!!

- These slides contains visual aids for learning BUT they are NOT the actual lecture notes!
- Failure to attend to lectures most probably result in failing the lecture!
- So I strongly recommend that you attend to the classes. Take a pen, a notebook and WRITE!

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## Chapter Objectives

- Describe the physical properties of gases.
- Identify several gaseous compounds or classes of compounds that are important in urban air pollution.
- Use the **ideal gas law** for calculating changes in the conditions of gases.
- Use the concept of **partial pressure** to work with mixtures of gases.

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## Chapter Objectives

- Perform stoichiometric calculations for reactions involving gases as reactants or products.
- State the postulates of the **kinetic theory of gases**.
- Describe qualitatively how the postulates of the kinetic theory account for the observed behavior of gases.
- Describe the **Maxwell-Boltzmann distribution** of speeds and the effects of temperature and molar mass on molecular speed.

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## Chapter Objectives

- Identify conditions under which gases might not behave ideally.
- Use the **van der Waals equation** to perform calculations for gases under nonideal conditions.
- Describe the principles of operation for some pressure-measuring devices.

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## Air Pollution

- Clean air is a mixture of several gases.

Table 5.1

The composition of a one cubic meter sample of dry air at 25°C and normal atmospheric pressure

Gas	# Moles Present
N <sub>2</sub>	31,929
O <sub>2</sub>	8,567
Ar	0,382
CO <sub>2</sub>	0,013
Other trace gases	0,002
Total	40,893

- Nitrogen and oxygen are major components
- Water vapor (humidity) varies with place, time, and temperature.
- Dry air is a convenient reference point

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## Air Pollution

- Six Principal **Criteria Pollutants**
  - CO, NO<sub>2</sub>, O<sub>3</sub>, SO<sub>2</sub>, Pb, and **Particulate Matter (PM)**
  - Commonly found throughout the country; cause a variety of negative effects on health, environment, and/or property.
- EPA established criteria for acceptable levels:
  - **Primary standards** intended to protect health.
    - **Nonattainment area**: region that exceeds primary standards
  - **Secondary standards** intended to protect environment and property.
- Allowable levels usually less than one **part per million (ppm)**.

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## Air Pollution

- The criteria pollutant nitrogen dioxide, NO<sub>2</sub>, is emitted by automobiles.
- High temperatures inside car engines cause oxygen and nitrogen to react to produce a variety of nitrogen oxides, designated with the generic formula NO<sub>x</sub>.
- Brown color of smog due to NO<sub>2</sub>; attacks lung membranes

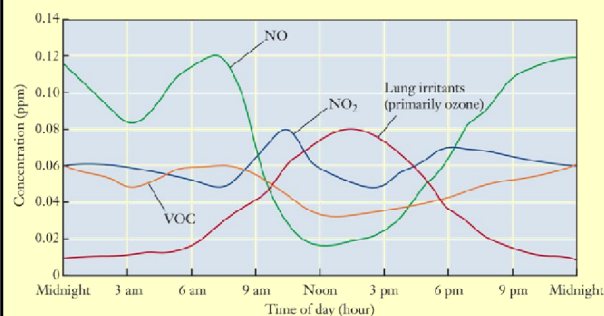
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## Air Pollution

- **Photochemical reactions**, reactions initiated by light energy, can trigger formation of ozone, another criteria pollutant, at ground level from:
  - nitrogen oxides
  - **volatile organic compounds (VOCs)**: hydrocarbons that readily evaporate
- Reactions between these two types of compounds produce a mixture a gases collectively referred to as smog.
  - Many components are lung irritants.
    - Ozone is the most significant lung irritant.

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## Air Pollution



- Pollutant levels vary with time of day and location.

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## Properties of Gases

- Expand to fill the volume of any container.
- Have much lower densities than solids or liquids.
- Have highly variable densities, depending on conditions.
- Mix with one another readily and thoroughly.
- Change volume dramatically with changing temperature.

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## Properties of Gases

- The **ideal gas law** is the quantitative relationship between pressure ( $P$ ), volume ( $V$ ), moles gas present ( $n$ ), and the absolute temperature ( $T$ ).
- $R$  is the **universal gas constant**.
  - $R = 0.08206 \text{ L atm mol}^{-1} \text{ K}^{-1}$ : used in most gas equations
  - $R = 8.314 \text{ J mol}^{-1} \text{ K}^{-1}$ : used in equations involving energy

$$PV = nRT$$

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### Pressure

- **Pressure** is force per unit area.  $P = \frac{F}{A}$
- Atmospheric pressure is the force attributed to the weight of air molecules attracted to Earth by gravity.
- As altitude increases, atmospheric pressure decreases.

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### Pressure

- Pressure results from molecular collisions between gas molecules and container walls.
- Each collision imparts a small amount of force.
- Summation of the forces of all molecular collisions produces the macroscopic property of pressure.

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### Measuring Pressure

- A **barometer** is used to measure atmospheric pressure.
- The height of the mercury column is proportional to atmospheric pressure.
- Units of Pressure
  - 1 torr = 1 mm Hg
  - 1 atm = 760 torr (exactly)
  - 1 atm = 101,325 Pa (exactly)
  - 760 torr = 101,325 Pa (exactly)

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### History and Application of the Gas Law

- Gases change significantly when the conditions in which they are found are altered.
- These changes are determined empirically using gas laws.
  - **Charles's Law**: relationship between  $T$  and  $V$
  - **Boyle's Law**: relationship between  $P$  and  $V$
  - **Avogadro's Law**: relationship between  $n$  and  $V$
- The empirical gas laws led to the ideal gas law

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### Charles's Law

- Jacques Charles studied relationship between volume and temperature.
- Plots of  $V$  versus  $T$  for different gas samples converged to the same temperature at zero volume.
  - Basis of the Kelvin temperature scale.

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### Charles's Law

- For fixed pressure and fixed number of moles of gas, the volume and the absolute temperature of a gas are directly proportional.

$$V \propto T$$

- All of the fixed variables can be factored out of the ideal gas law as a new constant that can be used to relate two sets of conditions:

$$\frac{V_1}{T_1} = \frac{nR}{P} = \text{constant} = \frac{V_2}{T_2}$$

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## Boyle's Law

- Pressure and volume are inversely proportional.

$$V \propto \frac{1}{P}$$

- All of the fixed variables can be factored out as a new constant that can be used to relate two sets of conditions:

$$P_1V_1 = nRT = \text{constant} = P_2V_2$$

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## Avogadro's Law

- Avogadro's Law states that for fixed pressure and temperature, the volume and moles of a gas are directly proportional.

$$V \propto n$$

$$\frac{V_1}{n_1} = \frac{RT}{P} = \text{constant} = \frac{V_2}{n_2}$$

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## Example Problem 5.1

- A common laboratory cylinder of methane has a volume of 49.0 L and is filled to a pressure of 154 atm. Suppose that all of the CH<sub>4</sub> from this cylinder is released and expands until its pressure falls to 1.00 atm. What volume would the CH<sub>4</sub> occupy?

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## Example Problem 5.2

- A balloon is filled with helium and its volume is 2.2 L at 298 K. The balloon is then dunked into a thermos bottle containing liquid nitrogen. When the helium in the balloon has cooled to the temperature of the liquid nitrogen (77 K), what will the volume of the balloon be?

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## Units and the Ideal Gas Law

- Temperature must be expressed in Kelvin for all gas calculations!
  - Negative temperatures would result in negative pressures, volumes, and moles.
  - In some engineering fields, the Rankine temperature scale is used, which is another absolute temperature scale.
    - 0°R = 0 K; 1°R = 1.8 K
- The unit for moles is always mol.
- The units for measuring pressure and volume can vary. In gas calculations, these units must agree with those of the gas constant
  - R = 8.314 J mol<sup>-1</sup> K<sup>-1</sup>
  - R = 0.08206 L atm mol<sup>-1</sup> K<sup>-1</sup>
  - R = 62.37 L torr mol<sup>-1</sup> K<sup>-1</sup>

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## Example Problem 5.3

- A sample of CO<sub>2</sub> gas has a volume of 575 cm<sup>3</sup> at 752 torr and 72°F. What is the mass of carbon dioxide in this sample?

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## Partial Pressure

- Air is a mixture of gases.
  - Gas laws do not depend on identity of gases.
  - Pressure due to total moles gas present.
- The pressure exerted by a component of a gas mixture is called the **partial pressure** for the component gas.

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## Partial Pressure

- Dalton's law of partial pressures:** The total pressure ( $P$ ) of a mixture of gases is the sum of the partial pressures of the component gases ( $P_i$ ).

$$P = \sum_i P_i$$

- Dalton's Law can be expressed in terms of **mole fraction**.
  - Mole fraction ( $X_i$ ) for a gas in a gas mixture is the moles of the gas ( $n_i$ ) divided by the total moles gas present.
  - The partial pressure of each gas is related to its mole fraction.

$$X_i = \frac{n_i}{n_{\text{total}}} \Rightarrow P_i = X_i P$$

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## Example Problem 5.4

- A scientist tries to generate a mixture of gases similar to a volcano by introducing 15.0 g of water vapor, 3.5 g of  $\text{SO}_2$ , and 1.0 g of  $\text{CO}_2$  into a 40.0 L vessel held at  $120.0^\circ\text{C}$ . Calculate the partial pressure of each gas and the total pressure.

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## Example Problem 5.5

- A mixture has the mole fractions given in the following table:

Gas	$\text{N}_2$	$\text{O}_2$	$\text{H}_2\text{O}$	$\text{SO}_2$
Mole Fraction	0.751	0.149	0.080	0.020

- If the desired pressure is 750. torr, what should the partial pressures be for each gas?
- If the gas is to be in a 15.0 L vessel held at  $30^\circ\text{C}$ , how many moles of each substance are needed?

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## Stoichiometry of Reactions Involving Gases

- For reactions involving gases, the ideal gas law is used to determine moles of gas involved in the reaction.
  - Use **mole ratios** (stoichiometry)
  - Connect number of moles of a gas to its temperature, pressure, or volume with ideal gas law

$$PV = nRT$$

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## Example Problem 5.6

- When an experiment required a source of carbon dioxide, a student combined 1.4 g of sodium bicarbonate ( $\text{NaHCO}_3$ ) with excess hydrochloric acid ( $\text{HCl}$ ). If the  $\text{CO}_2$  produced is collected at 722 torr and  $17^\circ\text{C}$ , what volume will the gas occupy?

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## STP Conditions

- Standard temperature and pressure, **STP**, for a gas is 0°C (273.15 K) and 1 atm.
- For one mole of gas at STP, the standard molar volume is 22.41 L (calculated using ideal gas law)
- This number provides a conversion factor for stoichiometric problems that include gases, *provided the STP conditions are maintained*.

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## Example Problem 5.7

- Carbon dioxide can be removed from a stream of gas by reacting it with calcium oxide to form calcium carbonate. If we react 5.50 L of CO<sub>2</sub> at STP with excess CaO, what mass of calcium carbonate will form?

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## Kinetic-Molecular Theory and Ideal versus Real Gases

- In many important practical settings, gases do not always behave ideally, especially at very high pressure and/or very low temperature.
- Nonideal gas behavior can be explained using **Kinetic Molecular Theory**.
  - Provides connections between observed macroscopic properties of gases, the gas law equation, and the behavior of gas molecules on a microscopic scale.

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## Postulates of the Model

- Gases are made up of large collections of particles, which are in constant, random motion.
- Gas particles are infinitely small and occupy negligible volume.
- Gas particles move in straight lines except when they collide with other particles or with the container walls. These collisions are elastic, so kinetic energy of particles is conserved.
- Particles interact with each other only when collisions occur.

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## Postulates of the Model

- The average kinetic energy of a gas is proportional to the absolute temperature of the gas but does not depend upon the identity of the gas

$$KE_{\text{avg}} = \frac{1}{2} m v_{\text{rms}}^2$$

- As temperature increases, average speed for gas molecules increases.
- Faster moving molecules collide more often and with greater force, exerting a higher pressure.

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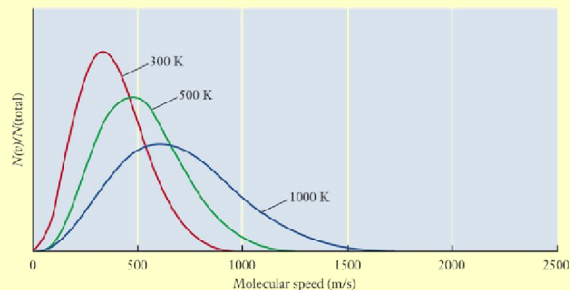
## Postulates of the Model

- At a given temperature, gas molecules in a sample can be characterized by an **average speed**.
  - Some gas molecules move faster than average, some move slower than average.
- The distribution function that describes the speeds of a collection of gas particles is known as the **Maxwell-Boltzmann distribution of speeds**.

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## Postulates of the Model

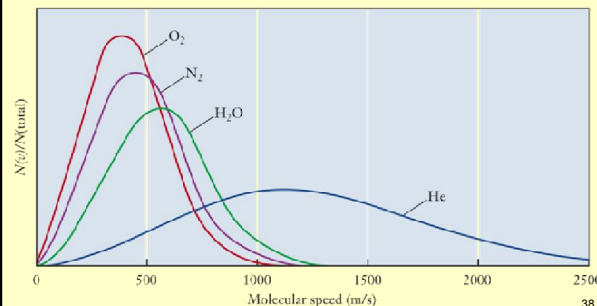
- As temperature increases, average speed increases.
  - As temperature increases, the fraction of molecules moving at higher speeds increases.



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## Postulates of the Model

- For a fixed temperature, as the molecular weight increases, the average speed for the gas molecules decreases.



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## Postulates of the Model

- The equation for the Maxwell-Boltzmann distribution describes  $N(v)$ , which is the number of molecules moving with speeds close to  $v$ .

$$\frac{N(v)}{N_{\text{total}}} = 4\pi \left( \frac{M}{2\pi RT} \right)^{3/2} v^2 e^{-Mv^2/2RT}$$

- Most gas molecules move at the most probable speed, which is the peak of the curve in the Maxwell-Boltzmann plot.

$$v_{\text{mp}} = \sqrt{\frac{2RT}{M}}$$

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## Postulates of the Model

- The Maxwell-Boltzmann distribution can be described in terms of the average speed or root-mean-square speed.

- Average speed,  $v_{\text{avg}}$ , is 1.128 times  $v_{\text{mp}}$ .
  - The existence of the "tail" on the distribution curve at high speeds will pull the average to a speed higher than the most probable value.
- $v_{\text{rms}} = 1.085$  times  $v_{\text{avg}}$ .
- The root-mean-square speed is useful because the average kinetic energy is given by  $\text{KE}_{\text{avg}} = \frac{1}{2} m v_{\text{rms}}^2$

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## Real Gases and Limitations of the Kinetic Theory

- Kinetic molecular theory implies that the volume of a gas molecule is insignificant compared to the "empty space" volume for a gas sample.
  - Mean free path used to test validity of assumption.
    - Average distance a particle travels between collisions with other particles.
    - The mean free path for air at room temperature and atmospheric pressure is 70 nm.
      - This value is 200 times larger than the typical radius of a small molecule like  $\text{N}_2$  or  $\text{O}_2$ .
    - Volume of empty space in a gas is 1 million times that of gas particle volume.

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## Real Gases and Limitations of the Kinetic Theory

- The volume of a gas particle is significant compared to the "empty space" volume under high pressure conditions.
  - Mean free path decreases as pressure increases.
  - Gas molecules are very close together.
- Therefore, volume of the gas particles becomes significant.

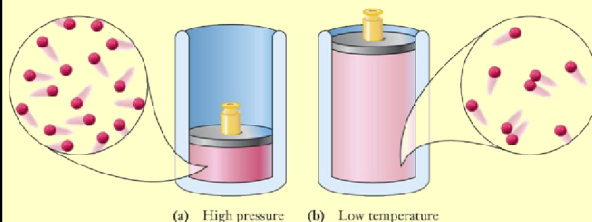
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### Real Gases and Limitations of the Kinetic Theory

- Kinetic molecular theory asserts that gas molecules move in straight lines and interact only through perfectly elastic collisions.
  - Gas molecules neither attract nor repel.
  - Strength of attractive forces small compared to kinetic energy of gas molecules.
- Attractive and repulsive forces are significant under conditions of low temperature.
  - Kinetic energy decreases with temperature.
  - Gas molecules experience "sticky" collisions.
  - Collision rate decreases, decreasing the pressure.

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### Real Gases and Limitations of the Kinetic Theory



- The ideal gas model breaks down at high pressures and low temperatures.
  - high pressure: volume of particles no longer negligible
  - low temperature: particles move slowly enough to interact

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### Correcting the Ideal Gas Equation

- **van der Waals equation** is commonly used to describe the behavior of real gases

$$\left(P + \frac{an^2}{V^2}\right)(V - nb) = nRT$$

- **a** corrects for attractive forces.
  - Molecules with stronger attractive forces have larger **a** values.
- **b** corrects for the volume occupied by gas molecules.
  - Large molecules have larger **b** values.

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### Correcting the Ideal Gas Equation

Table 5.2

Van der Waals constants for several common gases

Gas	$a$ ( $\text{atm L}^2 \text{mol}^{-2}$ )	$b$ ( $\text{L mol}^{-1}$ )
Ammonia, $\text{NH}_3$	4.170	0.03707
Argon, Ar	1.345	0.03219
Carbon dioxide, $\text{CO}_2$	3.592	0.04267
Helium, He	0.034	0.0237
Hydrogen, $\text{H}_2$	0.2444	0.02661
Hydrogen fluoride, HF	9.433	0.0739
Methane, $\text{CH}_4$	2.253	0.04278
Nitrogen, $\text{N}_2$	1.390	0.03913
Oxygen, $\text{O}_2$	1.360	0.03183
Sulfur dioxide, $\text{SO}_2$	6.714	0.05636
Water, $\text{H}_2\text{O}$	5.464	0.03049

- The van der Waals constants **a** and **b** are compound specific.

- Both are zero in gases behaving ideally.

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### Example Problem 5.8

- An empty 49.0 L methane storage tank has an empty mass of 55.85 kg and, when filled, has a mass of 62.07 kg. Calculate the pressure of  $\text{CH}_4$  in the tank at  $21^\circ\text{C}$  using both the ideal gas equation and the van der Waals equation.
- What is the percentage correction achieved by using the more realistic van der Waals equation?

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### Gas Sensors

- The concentration of air pollutants is monitored by the EPA.
  - The concentration of a gas is proportional to the partial pressure of the gas.
- Gas pressure sensors are used to monitor changes in partial pressure or concentration of gases.

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### Capacitance Manometer

- Changes in pressure cause deflections in the diaphragm, changing the capacitance.
- Used to measure pressures from 0.001 - 1000 torr

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### Thermocouple Gauge

- Measures pressure by the cooling effect of colliding gas molecules.
- Higher pressure, more collisions with heated filament, lowers filament temperature.
- Used to measure pressures from 0.01 to 1.0 torr

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### Ionization Gauge

- Pressure measured by producing gaseous cations with the electrons emitted from a hot filament.
- Higher pressure, more gas cations, more current collected at the grid.
- Used to measure pressures as low as  $10^{-11}$  torr.

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### Gas Sensors

- A thermocouple gauge, a capacitance manometer, and an ionization gauge.

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### Mass Spectrometers

- Mass spectrometers can be used to measure partial pressures for gas mixtures.
- Mass spectrometers ionize gas like an ionization gauge, but can select the mass of the gas being analyzed with the use of a magnetic field.
- Several masses can be scanned simultaneously allowing for multiple gas analyses.
- Current generated can be used to determine the partial pressure of gas.

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