

# Compatible ground-motion prediction equations for damping scaling factors and vertical-to-horizontal spectral amplitude ratios for the broader Europe region

S. Akkar · M. A. Sandıkkaya · B. Ö. Ay

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**Abstract** In a companion article Akkar et al. (Bull Earthq Eng, doi:10.1007/s10518-013-9461-4, 2013a; Bull Earthq Eng, doi:10.1007/s10518-013-9508-6, 2013b) present a new ground-motion prediction equation (GMPE) for estimating 5%-damped horizontal pseudo-acceleration spectral (PSA) ordinates for shallow active crustal regions in Europe and the Middle East. This study provides a supplementary viscous damping model to modify 5%-damped horizontal spectral ordinates of Akkar et al. (Bull Earthq Eng, doi:10.1007/s10518-013-9461-4 2013a; Bull Earthq Eng, doi:10.1007/s10518-013-9508-6, 2013b) for damping ratios ranging from 1 to 50%. The paper also presents another damping model for scaling 5%-damped vertical spectral ordinates that can be estimated from the vertical-to-horizontal (V/H) spectral ratio GMPE that is also developed within the context of this study. For consistency in engineering applications, the horizontal and vertical damping models cover the same damping ratios as noted above. The article concludes by introducing period-dependent correlation coefficients to compute horizontal and vertical conditional mean spectra (Baker in J Struct Eng 137:322–331, 2011). The applicability range of the presented models is the same as of the horizontal GMPE proposed by Akkar et al. (Bull Earthq Eng, doi:10.1007/s10518-013-9461-4 2013a; Bull Earthq Eng, doi:10.1007/s10518-013-9508-6, 2013b); as for spectral periods  $0.01 \text{ s} \leq T \leq 4 \text{ s}$  as

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S. Akkar (✉) · M. A. Sandıkkaya · B. Ö. Ay  
Department of Civil Engineering, Earthquake Engineering Research Center,  
Middle East Technical University, 06800 Ankara, Turkey  
e-mail: sakkar@metu.edu.tr

M. A. Sandıkkaya  
Institut des Sciences de la Terre (ISTerre), Université de Grenoble,  
38041 Grenoble, France

B. Ö. Ay  
European Centre for Training and Research in Earthquake Engineering,  
27100 Pavia, Italy

well as PGA and PGV for V/H model; and in terms of seismological estimator parameters  $4 \leq M_w \leq 8$ ,  $R \leq 200$  km,  $150 \text{ m/s} \leq V_{S30} \leq 1,200 \text{ m/s}$ , for reverse, normal and strike-slip faults. The source-to-site distance measures that can be used in the computations are epicentral ( $R_{\text{epi}}$ ), hypocentral ( $R_{\text{hyp}}$ ) and Joyner–Boore ( $R_{\text{JB}}$ ) distances. The implementation of the proposed GMPEs will facilitate site-specific adjustments of the spectral amplitudes predicted from probabilistic seismic hazard assessment in Europe and the Middle East region. They can also help expressing the site-specific design ground motion in several formats. The consistency of the proposed models together with the Akkar et al. (Bull Earthq Eng, doi:10.1007/s10518-013-9461-4 2013a; Bull Earthq Eng, doi:10.1007/s10518-013-9508-6, 2013b) GMPE may be advantageous for future modifications in the ground-motion definition in Eurocode 8 (CEN in Eurocode 8, Design of structures for earthquake resistance—part 1: general rules, seismic actions and rules for buildings. European Standard NF EN 1998-1, Brussels, 2004).

**Keywords** Damping scaling factors · Vertical-to-horizontal spectral amplitudes · Ground motion prediction equations for pan-European region · Conditional mean spectrum

## 1 Introduction

Base isolated structures, tall buildings and buildings with supplementary damping devices as well as the simplified equivalent linear procedures that mimic the nonlinear response of structures require scaling of commonly provided 5%-damped response spectrum to different damping levels. In addition, the vertical seismic hazard becomes crucial especially for short-period critical structural facilities (e.g., nuclear power plants and dams) that are prone to structural damage upon the exceedance of a certain level of vertical displacement (Campbell and Bozorgnia 2003; Gülerce and Abrahamson 2011; Bommer et al. 2011). The vertical ground motions have also been identified as important for the design of lifeline systems and ordinary short-period structures in the vicinity of the fault (Elnashai and Papazoglu 1997; Kunnath et al. 2008; Gülerce and Abrahamson 2011). Thus, proper predictive models for describing vertical ground-motion demands and elastic spectral ordinates at different damping levels are always needed in the engineering community.

A detailed review on viscous damping scaling models for estimating spectral ordinates other than 5% of critical is given in Rezaeian et al. (2012) and ATC (2010).<sup>1</sup> Currently, modern seismic design codes and guidelines suggest multiplicative factors to scale the 5%-damped elastic spectral ordinates into ordinates for other damping ratios by period-independent tabulated values (e.g., NEHRP 2009)<sup>1</sup> or simple period-dependent expressions (e.g., Eurocode 8; CEN 2004). These simplified factors or expressions aggregate the likely influence of seismological parameters from a broad perspective. Consequently, their implementation to site-specific (or project-specific) probabilistic seismic hazard assessment (PSHA) may not always describe the accurate period-dependent variation of spectral ordinates for different damping levels.

The evolutionary progress in vertical design spectrum is summarized by Bommer et al. (2011) and Bozorgnia and Campbell (2004). Although it was common to use the ratio of 2/3 between vertical and horizontal design spectra in the past codes [based on the findings of Newmark and Hall (1982)], the recent seismic codes (e.g., NEHRP and Eurocode 8) acknowledge the period-dependent differences in the spectral shapes of horizontal and vertical design spec-

<sup>1</sup> ATC is Applied Technology Council and NEHRP is National Earthquake Hazards Reduction Program.

tra because the frequency content, magnitude- and distance-dependent scaling of horizontal and vertical ground motions differ. The aforementioned codes define simplified vertical-to-horizontal (V/H) spectral ratios that are conditioned on PGA (Eurocode 8) and PSA at  $T = 0.2$  s (NEHRP). Though conceptually different, the period-dependent V/H spectral ratios defined by these codes consider magnitude and source-to-site distance effects on vertical design spectrum. The NEHRP provisions also consider the influence of site class on the V/H ratios whereas differences in site class are assumed to be insignificant in Eurocode 8. For practical reasons, the above described generic V/H ratios can be of use for defining vertical code-based spectrum. However, such oversimplified expressions are not appropriate for site-specific probabilistic hazard studies. PSHA requires consistent and compatible earthquake scenarios for horizontal and vertical ground motions that are determined through scenario spectrum (computed from deaggregation of hazard at a specific period) or conditional mean spectrum, CMS (Baker 2011). [The reader is referred to Gülerce and Abrahamson (2011) for extended discussions on the implementation of V/H GMPEs to scenario spectrum and CMS]. This point is even more important if vertical and horizontal acceleration time series have to be selected and scaled for the target hazard levels. For such cases, empirical V/H spectral ratio models are required for a proper mapping of source, path and site effects on to V/H ratios. Moreover, such complete V/H GMPEs would be beneficial for further improvements in code-based generic V/H spectral ratio expressions.

This paper describes a set of ground-motion predictive models for scaling 5%-damped horizontal and vertical spectral ordinates for viscous damping ratios varying between 1 and 50%. The chosen damping range can sufficiently address the needs of most seismic design and performance assessment projects. The paper also describes a model for predicting the ratios of vertical-to-horizontal 5%-damped PSA ordinates. These predictive models are derived from the ground-motion database used by Akkar et al. (2013a,b) that developed a GMPE for horizontal PSA for its use in the seismic hazard assessment of shallow active crustal regions in Europe and the Middle East. Having been developed from the same pan-European ground-motion database with the same spectral period interval and capable of addressing different distance metrics, the predictive models presented in this paper are the first fully compatible GMPEs for producing consistent scenario-based horizontal and vertical design spectra at different damping levels that can be of use in many engineering applications in the broader Europe region. The applicability range of the proposed models in this paper is similar to the horizontal Akkar et al. (2013a,b) GMPE. This property can be useful in future studies to update the definitions of horizontal and vertical ground-motion demands in Eurocode 8 (CEN 2004). The paper also introduces the epsilon-based correlation coefficients that are used for developing horizontal and vertical conditional mean spectra (CMS); a concept proposed by Baker (2011) that accounts for the period-dependent variability of ground motion for scenario spectrum. The proposed models, together with the horizontal Akkar et al. (2013a,b) GMPE can also be used in vector-valued PSHA (Bazzurro and Cornell 2002) in Europe and surrounding regions.

## 2 Strong-motion database

The strong-motion accelerograms used in this study are selected from RESORCE (Akkar et al. 2013c). RESORCE is developed for the Seismic Ground Motion Assessment (SIGMA; <http://projet-sigma.com/index.html>) project and it is the updated and extended version of the pan-European databases compiled under the Seismic Hazard HARMONIZATION in Europe (SHARE) project (Yenier et al. 2010). The database consists of 1,041 accelerograms recorded

from 221 shallow active crustal earthquakes. The epicentral locations of most of these events cover the Mediterranean region and the Middle East. The moment magnitudes ( $M_w$ ) of recordings range between 4 and 7.6 and their source-to-site distances ( $R_{JB}$ ; closest distance between the vertical projection of ruptured fault and site) are up to 200 km. The strong-motion records in the database have the complete information on epicentral ( $R_{epi}$ ) and hypocentral ( $R_{hyp}$ ) distances as well. The site conditions of all accelerograms are identified by measured  $V_{S30}$  (time based average shear-wave velocity of the upper 30 m soil layer). The  $V_{S30}$  interval of the database is between 92 and 2,165 m/s. The database consists of normal, reverse and strike-slip earthquakes of focal depths less than 30 km. Only three-component accelerograms recorded at free-field stations are used. Singly recorded events are removed from the database. The reader is referred to [Akkar et al. \(2013a,b\)](#) for the overall and specific features of the strong-motion database as it is common for both studies.

The horizontal and vertical PSA at 16 different damping levels (i.e., 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 15, 20, 25, 30, 40 and 50 %) are computed from the compiled strong-motion database to develop the GMPEs for damping scaling and V/H spectral ratios. The dense damping distribution towards lower damping levels is a modeling requirement for a better fit on the observed data. The geometric means of horizontal PGA, PGV and 62 spectral ordinates ( $0.01 \text{ s} \leq T \leq 4.0 \text{ s}$ ) represent the horizontal ground-motion demands in the proposed GMPEs. The selected spectral periods are the same as those used in [Akkar et al. \(2013a,b\)](#). This way full compatibility is provided between the models developed here and the GMPE for the horizontal PSA presented in [Akkar et al. \(2013a,b\)](#). The usable spectral period band of each accelerogram is computed by using the criteria set in [Akkar and Bommer \(2006\)](#).

### 3 Predictive equations for damping scaling factors

[Bommer and Mendis \(2005\)](#), [Lin et al. \(2005\)](#) and [Rezaeian et al. \(2012\)](#) give a detailed literature review on the predictive models for damping scaling factor (DSF). As shown in Eq. (1), DSF is the normalized PSA of different damping levels ( $\beta$ ) with PSA at 5 % damping.

$$DSF = \frac{\text{PSA at } \beta\% \text{ damping}}{\text{PSA at } 5\% \text{ damping}} \quad (1)$$

Most of the previous DSF models are either built on  $\beta$  (e.g., [Ashour 1987](#); [Tolis and Faccioli 1999](#); [Priestly 2003](#); NEHRP) or  $\beta$  together with spectral period,  $T$ , (e.g., [Newmark and Hall 1982](#); [Wu and Hanson 1989](#); [Idriss 1993](#); [Naeim and Kircher 2001](#); [Ramirez et al. 2000, 2002](#); [Lin and Chang 2003](#); [Atkinson and Pierre 2004](#); [Malhotra 2006](#); Eurocode 8). Few models discussed the effects of other independent parameters on DSF. [Stafford et al. \(2008\)](#) emphasized the significance of duration whereas [Abrahamson and Silva \(1996\)](#) included  $M_w$  as an additional predictor variable in their model. [Lin and Chang \(2004\)](#) and [Hatzigeorgiou \(2010\)](#) indicated the role of site class on DSF and considered this parameter in their functional forms. [Cameron and Green \(2007\)](#) modeled the influence of tectonic regime in their damping scaling relationship together with other important estimator parameters such as  $M_w$ , site class and source-to-site distance. The most recent study conducted by [Rezaeian et al. \(2012\)](#) showed that magnitude, source-to-site distance and spectral period are sufficient for unbiased DSF estimates.

In this study, the natural logarithm of DSF is regressed against  $M_w$ ,  $R_{JB}$ , SoF (style-of-faulting) and  $V_{S30}$  for each damping level and period. Other estimator parameters (e.g., duration) are not included to keep the model as simple as possible for lesser complexity in hazard studies. The [Akkar et al. \(2013a,b\)](#) functional form is chosen as the backbone

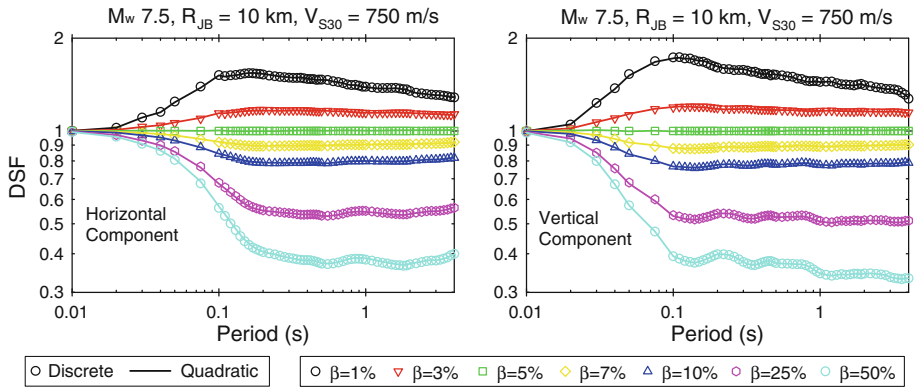
expression for the DSF model. The magnitude scaling in Akkar et al. (2013a,b) is quadratic with a break in the linear term whereas a magnitude-dependent geometrical spreading is considered to account for path effects. The site term in Akkar et al. (2013a,b) is composed of linear and nonlinear terms for a realistic modeling of soil behavior. Akkar et al. (2013a,b) address the SoF effects on ground-motion amplitudes by dummy variables for normal and reverse events over strike-slip earthquakes. The preliminary regression results showed that the bilinear magnitude scaling function or consideration of higher order magnitude terms in the backbone functional form do not increase the accuracy of DSF estimates. The magnitude-dependent slope term in geometrical spreading also did not play an efficient role on the distance scaling of median DSF trends. None of these complicated functions in magnitude and distance scaling decreased the standard deviation (aleatory variability) of the model. The style-of-faulting effect is also disregarded in the final model as DSF is insensitive to different faulting mechanisms. The averages of residual distributions for each SoF are almost zero that also justifies the decision to disregard the SoF terms in the final DSF model. It should be noted that the non-uniform SoF distribution in the strong-motion database may mask the actual effect of this parameter on DSF. Thus, overlooking the SoF effect in the DSF predictive model can increase the epistemic uncertainty in our DSF estimates. The fictitious depth term in distance scaling is also kept constant for all spectral periods to have a smooth variation in the spectral shape. Consideration of fictitious depth as a period-dependent parameter did not change the model estimates, which advocates its marginal effect on DSF estimates. The nonlinear site amplification term is dropped after the first round of regression analyses as the variation of DSF is independent of nonlinear soil behavior. Thus, the modification of DSF amplitudes due to different soil conditions is described by the linear site term. The linear site term is constrained to a constant value for  $V_{S30} > 1,000$  m/s. The  $V_{S30}$  for reference rock condition is defined as  $V_{REF} = 750$  m/s in the site term. The final functional form of the DSF ground-motion model is given in Eq. (2).

$$\ln(DSF) = c_1 + c_2(M_w - 6.75) + c_3 \ln\left(\sqrt{R_{jB}^2 + c_5^2}\right) + c_4 \ln\left[\frac{\min(V_{S30}, 1,000)}{V_{REF}}\right] \quad (2)$$

In the above expression,  $c_i$  ( $i = 1-4$ ) denotes period-dependent regression coefficients computed by mixed-effects regression procedure (Abrahamson and Youngs 1992). They are smoothed by moving average technique to prevent jagged DSF trends. The regression coefficient  $c_5$  is the fictitious depth term and it is taken as constant ( $c_5 = 5$ ) for the entire period range for horizontal and vertical DSF models. The previous models for DSF (e.g., Trifunac and Lee 1989; Boore et al. 1993; Bommer et al. 1998; Berge-Thierry et al. 2003; Faccioli et al. 2004; Akkar and Bommer 2007) provide different sets of regression coefficients for each damping level. This approach is not followed in this study. Each regression coefficient  $c_i$  ( $i = 1-4$ ) is represented by a quadratic function in terms of natural logarithm of  $\beta$  (in percent) as given in Eq. (3).

$$c_i = b_{i1} + b_{i2} \ln(\beta / 5) + b_{i3} [\ln(\beta / 5)]^2 \quad (3)$$

The primary aim of this approach is to increase the applicability of the model. Newmark and Hall (1982) are the first proponents of such polynomial functions. In their paper, Newmark and Hall (1982) proposed a linear function. We tried polynomial functions of different orders. The observations from these trials indicated that the quadratic function (Eq. 3) is sufficient to explain the data trend. Rezaeian et al. (2012) also use a quadratic expression in their damping model. Figure 1 compares the performance of Eq. (3) with the discrete DSF estimates that are directly obtained from regressions on Eq. (2). The comparisons are done for different damping levels and for a strike-slip earthquake scenario of  $M_w$  7.5. The rock site ( $V_{S30} =$



**Fig. 1** Discrete damping scaling factors obtained from direct regressions on Eq. (2) for each damping level and their comparisons with those computed from Eq. (3) that describes each regression coefficient in Eq. (2) as a quadratic function

750 m/s) is located at a distance of  $R_{JB} = 10$  km from the causative fault. The left and right panels show the comparisons for horizontal and vertical spectral components, respectively. The patterns between the comparative plots overlap with each other that certify the success of Eq. (3) in representing the regression coefficients  $c_i$  ( $i = 1 - 4$ ) to estimate DSFs for different damping values. The rational functional form of Bommer et al. (1998) that is used in Eurocode 8 was also evaluated as an alternative to Eq. (3) while developing the proposed DSF model. However, it was discarded in the later stages of the study because the resultant DSF estimates were unrealistic. Table 1 presents the horizontal spectral ordinate DSF regression coefficients  $b_{ij}$  for each  $c_i$  for a set of selected spectral periods. The index  $i$  varies from 1 to 4 whereas  $j$  takes values between 1 and 3. In a similar way, Table 2 lists the same regression coefficients for the DSF model of vertical spectral ordinates.

The within-event ( $\phi$ ) and between-event ( $\tau$ ) standard deviations are computed by using quadratic expressions that are given in Eq. (4). The total standard deviation ( $\sigma$ ) is the square root of the sum of the squares of within-event and between-event standard deviation terms. The regression coefficients of within- and between-event standard deviations for horizontal and vertical DSF models are given in Tables 3 and 4, respectively for the periods listed in Tables 1 and 2. The model regression coefficients for the full list of spectral ordinates are available in the electronic supplement to this article.

$$\phi = b_{61} + b_{62} \ln(\beta / 5) + b_{63} [\ln(\beta / 5)]^2 \tag{4a}$$

$$\tau = b_{71} + b_{72} \ln(\beta / 5) + b_{73} [\ln(\beta / 5)]^2 \tag{4b}$$

$$\sigma = \sqrt{\phi^2 + \tau^2} \tag{4c}$$

Figure 2 shows the magnitude, distance and  $V_{S30}$  dependent variations of the proposed DSF model for horizontal (left column) and vertical (right column) PSA ordinates at  $T = 0.1$  s. The effect of damping is prominent at short spectral periods, which is the main reason for choosing  $T = 0.1$  s in this illustrative case. The effect of magnitude scaling on DSF is presented on the 1st row for a stiff site ( $V_{S30} = 525$  m/s) located at a distance of  $R_{JB} = 15$  km from the causative fault. The magnitude influence is more visible on horizontal ground motions when  $\beta$  attains larger values. The variations in DSF for vertical spectral ordinates are less sensitive to magnitude. However, as in the case of horizontal DSF model, magnitude effect starts contributing to vertical DSF variations for heavily damped structural systems (i.e.,

**Table 1** DSF regression coefficients for horizontal spectral ordinates

Period (s)	b <sub>11</sub>	b <sub>12</sub>	b <sub>13</sub>	b <sub>21</sub>	b <sub>22</sub>	b <sub>23</sub>	b <sub>31</sub>	b <sub>32</sub>	b <sub>33</sub>	b <sub>41</sub>	b <sub>42</sub>	b <sub>43</sub>
0.01	0.001198	-0.00358	-0.00124	0.00004	0.000045	0.000595	-0.00032	0.000585	0.00005	-0.0001	0.001432	-0.00111
0.02	0.001663	-0.03478	-0.00165	-0.00042	0.000684	0.000079	-0.00032	0.007236	0.00023	0.000387	-0.00046	-0.00059
0.03	0.005268	-0.10669	0.006535	-0.00041	0.002418	0.001401	-0.00093	0.021327	-0.00128	0.000664	-0.01002	-0.00047
0.04	0.003168	-0.16643	0.005757	-0.00068	0.014843	0.00156	-0.00015	0.032546	-0.00059	0.00105	-0.02782	0.000878
0.05	0.001719	-0.23363	0.00509	-0.00017	0.019448	0.005037	0.000518	0.043221	0.000537	0.001386	-0.0365	-8.2E-05
0.075	-0.00246	-0.33204	-0.00979	-0.00025	0.031044	0.008748	0.001643	0.051293	0.005062	0.00189	-0.04572	-0.00212
0.10	0.001867	-0.37117	-0.03101	0.000455	0.028815	0.011975	0.000706	0.040656	0.010132	0.001147	-0.07169	-0.00393
0.15	-0.00138	-0.38038	-0.06364	-0.00135	0.022613	0.011994	0.00053	0.025346	0.013599	-0.00053	-0.05921	-0.01104
0.20	0.001431	-0.33998	-0.06977	-0.00175	0.014247	0.011454	-0.00042	0.005123	0.011979	0.002233	-0.03628	-0.01206
0.30	0.005664	-0.28422	-0.06911	-0.00202	0.002101	0.009863	-0.00115	-0.01348	0.008246	0.000096	-0.01385	-0.01315
0.40	0.008775	-0.247	-0.06433	-0.00203	-0.00671	0.006677	-0.00158	-0.02594	0.005468	0.001794	-0.00354	-0.007
0.50	0.005547	-0.23394	-0.06448	-0.00209	-0.01892	0.003051	-0.0008	-0.02792	0.005283	-0.0009	0.015135	-0.00043
0.75	0.008193	-0.1923	-0.05717	-0.00095	-0.02443	-0.00206	-0.00122	-0.0358	0.002565	0.000301	0.039576	0.004235
1.00	0.00392	-0.17601	-0.04841	-0.00052	-0.03092	-0.00581	-0.0003	-0.03733	-0.00061	-0.00112	0.044602	0.00561
1.50	0.004771	-0.16221	-0.04924	0.000871	-0.04225	-0.01033	-0.00037	-0.04071	-0.00146	-0.00024	0.036168	0.003788
2.00	0.007292	-0.1398	-0.05212	0.000892	-0.04892	-0.01261	-0.00091	-0.04492	-0.00108	-0.00017	0.016833	0.001299
3.00	0.005723	-0.11785	-0.0493	0.001401	-0.05677	-0.01428	-0.00061	-0.04518	-0.00246	-0.00018	0.004307	-0.00283
4.00	0.011176	-0.10534	-0.04561	0.002951	-0.06213	-0.01519	-0.00186	-0.04301	-0.00308	0.002149	0.01449	0.000704

**Table 2** DSF regression coefficients for vertical spectral ordinates

Period (s)	b <sub>11</sub>	b <sub>12</sub>	b <sub>13</sub>	b <sub>21</sub>	b <sub>22</sub>	b <sub>23</sub>	b <sub>31</sub>	b <sub>32</sub>	b <sub>33</sub>	b <sub>41</sub>	b <sub>42</sub>	b <sub>43</sub>
0.01	0.002398	-0.00464	-0.00233	0.000134	0.000824	0.000178	-0.00054	0.001026	0.000096	-0.00034	0.001767	-0.00042
0.02	0.005533	-0.06364	-0.00289	-0.00043	0.000809	-0.00031	-0.00111	0.012461	0.000398	0.000423	-0.00315	-0.00015
0.03	0.010098	-0.21702	0.006742	0.000278	0.002155	0.001846	-0.0016	0.041863	-0.00077	0.000357	-0.01709	0.001313
0.04	0.005007	-0.34911	-8.2E-05	0.000571	0.008769	0.002005	-0.00098	0.06518	0.00136	-0.00392	-0.02208	0.000569
0.05	-0.0058	-0.4374	-0.00941	-0.00086	0.006867	0.002161	0.001963	0.075147	0.005143	-0.0016	-0.02277	0.006149
0.075	-0.00277	-0.48161	-0.03847	0.000331	0.009436	0.008139	0.001848	0.063017	0.012584	0.002601	-0.01395	0.000355
0.10	-0.00546	-0.5014	-0.05565	-0.00024	0.005231	0.008305	0.001058	0.054456	0.013547	-0.00459	-0.01566	-0.00549
0.15	-0.00232	-0.43125	-0.06884	-0.0023	0.004934	0.011808	-0.0004	0.025253	0.014911	-0.00146	-0.01647	-0.00384
0.20	0.000263	-0.36461	-0.06749	-0.00213	0.011499	0.013214	-0.00065	0.006098	0.013541	-0.0021	-0.00182	-0.00047
0.30	0.003355	-0.33041	-0.06519	-0.00165	-0.00078	0.010869	-0.00156	-0.00524	0.009268	-0.00119	0.003087	-0.000831
0.40	0.003602	-0.29517	-0.06264	-0.00109	-0.00217	0.007274	-0.00026	-0.014	0.006229	0.001091	0.010125	-0.00098
0.50	0.00246	-0.27448	-0.05932	-0.00258	-0.00901	0.005028	-0.00064	-0.0204	0.0055	-0.00021	0.02152	-0.00359
0.75	0.001086	-0.25524	-0.05557	0.000542	-0.01312	-0.00124	0.000952	-0.02097	0.002209	0.000718	0.031537	0.00227
1.00	0.001147	-0.23412	-0.05651	-0.00035	-0.02405	-0.00721	-0.00027	-0.02944	0.000776	-0.00256	0.017635	0.006128
1.50	0.005222	-0.21514	-0.06118	0.00074	-0.03342	-0.01028	-0.00088	-0.03177	0.001425	-0.00172	0.02434	0.00653
2.00	0.002785	-0.20364	-0.05809	0.001242	-0.04422	-0.01025	-0.00032	-0.03204	0.000413	-0.0018	0.017399	0.003592
3.00	0.006202	-0.19389	-0.06675	0.001639	-0.05576	-0.01244	-0.00054	-0.03002	0.001253	0.000168	-0.00426	-0.00249
4.00	0.009549	-0.16484	-0.0776	0.001935	-0.06004	-0.01763	-0.00185	-0.03143	0.002593	-0.00107	-0.0094	-0.00754

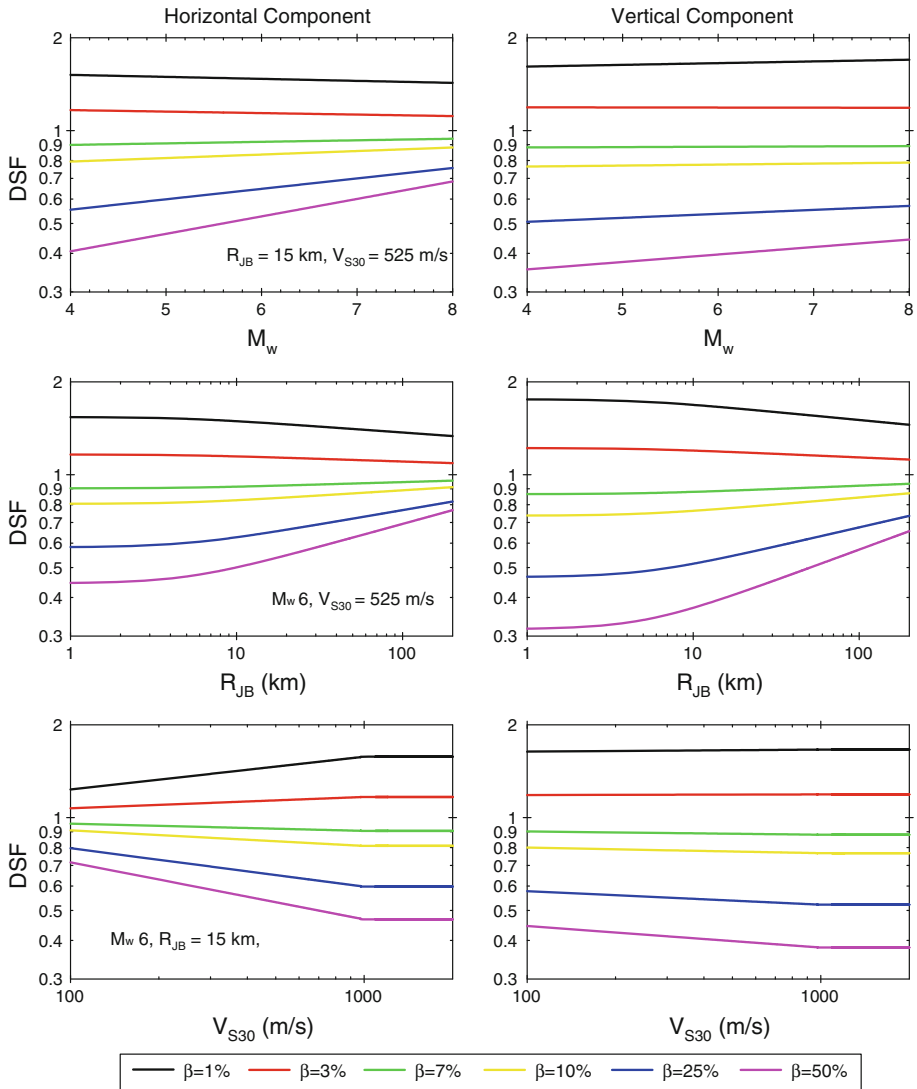


**Table 3** Standard deviation regression coefficients of the DSF model for horizontal spectral ordinates

Period (s)	b <sub>61</sub>	b <sub>62</sub>	b <sub>63</sub>	b <sub>71</sub>	b <sub>72</sub>	b <sub>73</sub>
0.01	0.005265	0.000924	0.005494	0.003564	-0.00135	0.002088
0.02	0.014935	-0.00456	0.013462	0.005076	-0.00226	0.003633
0.03	0.035034	-0.00757	0.028221	0.008231	-0.00048	0.009057
0.04	0.052255	-0.00348	0.039481	0.015437	-0.00198	0.01255
0.05	0.058578	-0.00406	0.044772	0.010115	0.000274	0.013369
0.075	0.068836	0.000203	0.050315	0.011068	0.005923	0.016025
0.10	0.065102	0.001334	0.050329	0.015893	0.000911	0.018006
0.15	0.062401	0.004246	0.049681	0.00669	0.004142	0.011661
0.20	0.064469	0.004089	0.046537	0.006733	0.004407	0.011793
0.30	0.061431	0.004647	0.045281	0.008272	0.000026	0.012741
0.40	0.062847	0.005084	0.044374	0.005145	0.000695	0.013102
0.50	0.058855	0.002856	0.044091	0.012835	0.002618	0.016743
0.75	0.064181	0.006075	0.044561	0.008911	-0.00132	0.013721
1.00	0.063034	0.005479	0.045448	0.016261	0.001629	0.015567
1.50	0.06232	0.002838	0.04653	0.012108	0.009527	0.017909
2.00	0.058796	0.008895	0.046878	0.008415	0.004801	0.01597
3.00	0.052093	0.011071	0.042998	0.01788	0.006693	0.022389
4.00	0.047785	0.014943	0.041903	0.0197	0.015215	0.021287

**Table 4** Standard deviation regression coefficients of the DSF model for vertical spectral ordinates

Period (s)	b <sub>61</sub>	b <sub>62</sub>	b <sub>63</sub>	b <sub>71</sub>	b <sub>72</sub>	b <sub>73</sub>
0.01	0.002946	-0.0008	0.002973	0.001733	-0.00104	0.001661
0.02	0.009187	-0.00222	0.008102	0.002404	-0.00088	0.002426
0.03	0.017113	-0.0047	0.016379	0.005133	-0.00051	0.00511
0.04	0.025923	-0.00359	0.022437	0.011986	-0.00225	0.010168
0.05	0.034072	-0.0022	0.029385	0.013388	0.002185	0.013223
0.075	0.049981	0.000757	0.041528	0.015192	0.003326	0.018309
0.10	0.049716	0.002192	0.042586	0.018613	0.008826	0.020338
0.15	0.051899	0.007075	0.047045	0.013493	0.007444	0.015328
0.20	0.04933	0.00793	0.043589	0.009903	0.01014	0.012507
0.30	0.048411	0.005822	0.040023	0.000065	0.000723	0.012317
0.40	0.047006	0.008451	0.038979	0.006417	0.001097	0.012472
0.50	0.046804	0.005188	0.037081	0.00964	0.001451	0.011667
0.75	0.046953	0.007885	0.038768	0.012584	0.001159	0.015274
1.00	0.049176	0.006004	0.040136	0.00439	0.006055	0.012511
1.50	0.047777	0.009043	0.042481	0.013316	0.006169	0.016945
2.00	0.046394	0.011464	0.040939	0.01072	0.006785	0.015758
3.00	0.043665	0.010874	0.038291	0.014682	0.013664	0.020779
4.00	0.040025	0.014647	0.036967	0.017957	0.015872	0.02218



**Fig. 2** Magnitude (*first row*), distance (*second row*) and  $V_{S30}$  (*third row*) dependent variation of horizontal (*left panel*) and vertical (*right panel*) DSF at  $T = 0.1$  s

$\beta \geq 20\%$ ). Distance-dependent scaling of DSF is plotted in the 2nd row on Figure 2 for  $M_w = 6$  and  $V_{S30} = 525$  m/s. The effect of distance on DSF seems to be more apparent than the influence of magnitude. The decay due to geometrical spreading of DSF is faster at very low ( $\beta < 3\%$ ) and high ( $\beta > 15\%$ ) damping ratios. The 3rd row plots on Figure 2 shows the  $V_{S30}$  scaling of DSF for a scenario event of  $M_w = 6$  and  $R_{JB} = 15$  km. The damping scaling of horizontal ground motions grows with increasing  $V_{S30}$  up to 1,000 m/s and becomes stable after  $V_{S30} = 1,000$  m/s (imposed by the site model). This trend is more visible at lower and higher damping ratios. As in the case of magnitude, the damping scaling of vertical spectrum becomes sensitive to the changes in  $V_{S30}$  when  $\beta$  attains larger values (i.e.,  $\beta \geq 20\%$ ).

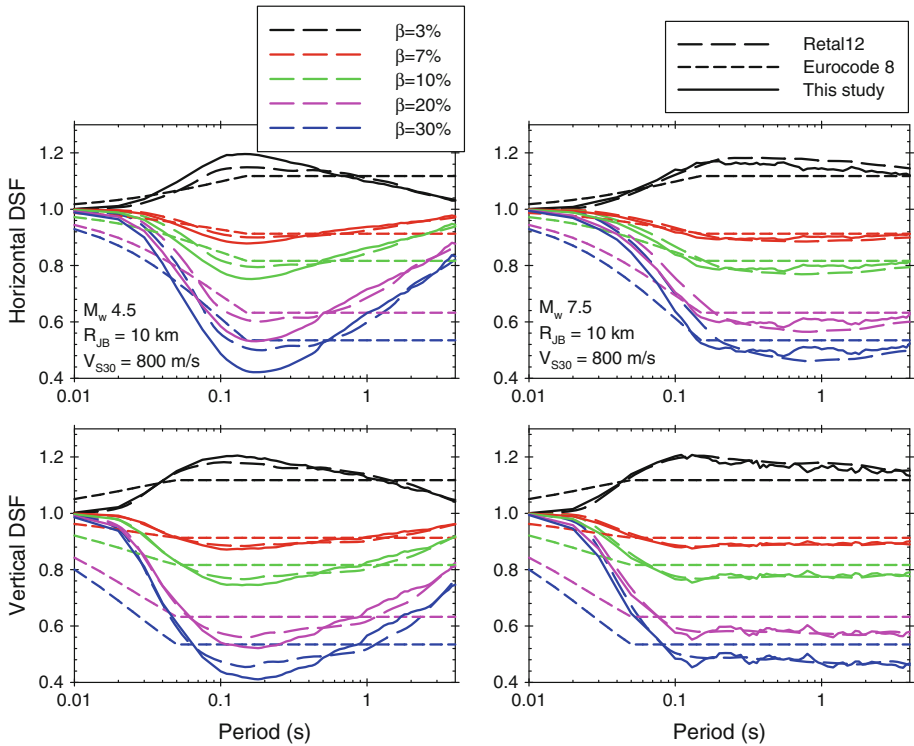
Figure 3 compares the horizontal (top row) and vertical (bottom row) DSF models with those of Rezaeian et al. (2012) and Eurocode 8 (CEN 2004). The Rezaeian et al. (2012) model is abbreviated as Retal12 on the plots. The comparisons are made for two different magnitudes:  $M_w$  4.5 (left column) and  $M_w$  7.5 (right column) that resemble low seismicity (Type II) and high seismicity (Type I) regions, respectively according to Eurocode 8. The fictitious site is selected as a generic rock site with  $V_{S30} = 800$  m/s. It is located at a distance of  $R_{JB} = 10$  km from a 90 degrees dipping strike-slip fault. The top of the ruptured fault segment is assumed to be 5 km below the surface for both cases. Under this simple source geometry the corresponding rupture distance ( $R_{rup}$ ; the distance measure used in the Retal12) is computed as 11.2 km. The comparative plots indicate that DSF estimates of this study and Retal12 agree with each other fairly well. There are differences in the DSF values of Eurocode 8 and the other two GMPEs. The Eurocode 8 damping scaling is sensitive to period variation only in the very short spectral period range. The other two DSF models consider the period influence on damping for the entire period band. This conceptual difference between Eurocode 8 and the other two DSF models show itself particularly in low seismicity regions (mimicked by  $M_w$  4.5), towards longer periods ( $T > 1.0$  s) and when  $\beta$  attains large values. For short-period spectral regions, the two DSF models tend to estimate larger spectral ordinates with respect to Eurocode 8. The less conservative short-period Eurocode 8 damping scaling is prominent in vertical spectral ordinates and at large damping values. These discussions advocate the reconsideration of damping scaling in the future modifications of Eurocode 8 ground-motion definition.

The last figure (Fig. 4) in this section shows the significance of aleatory variability in DSF estimates. The left and right panels in Fig. 4 depict median and  $\pm$  sigma horizontal and vertical DSF estimates of the proposed model for  $\beta = 1$  and 10%. The chosen scenario event has a moment magnitude of  $M_w$  7.0; however, it is noted that our sigma is independent of magnitude. The site resembles stiff soil conditions ( $V_{S30} = 400$  m/s) and it is located  $R_{JB} = 10$  km from a strike-slip fault. The comparative plots indicate that the aleatory variability is more significant in vertical DSF amplitudes.

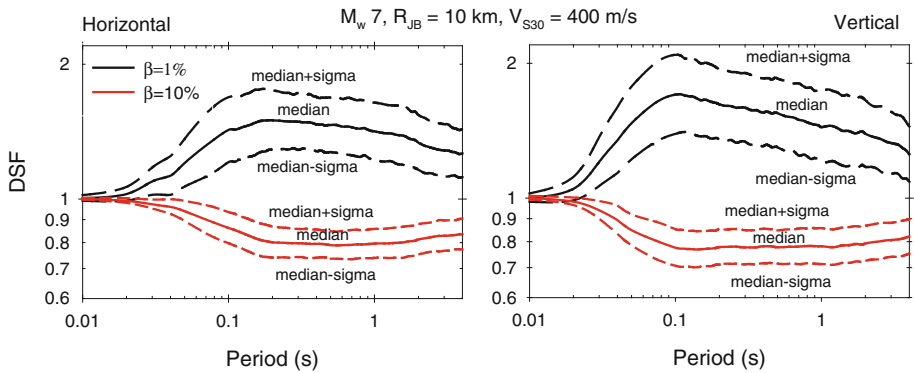
#### 4 Vertical-to-horizontal (V/H) spectral amplitude predictive model

The vertical-to-horizontal PSA GMPE presented in this section differs from the recently proposed vertical ground-motion models in Europe.<sup>2</sup> The proposed model is capable of estimating V/H ratios for all site conditions that makes it different from the V/H models of Edwards et al. (2011) and Poggi et al. (2012) that are valid for rock and soft sites, respectively. Although the empirical V/H model proposed in this study as well as the one proposed by Bommer et al. (2011) are based on European datasets, the GMPE of this study is developed on a more comprehensive and recently revised pan-European ground-motion database (Akkar et al. 2013c). The other major difference between the V/H model of this study and Bommer et al. (2011) is the site response function. The site term of our model is a continuous function of  $V_{S30}$  and considers soil nonlinearity whereas Bommer et al. (2011) use a set of dummy parameters to account for the site effects. Besides, the proposed V/H model is fully compatible with the pan-European 5%-damped horizontal PSA GMPE of Akkar et al. (2013a,b) because the database, thus all metadata and record processing, is common in both models. This property makes our model more useful in probabilistic seismic hazard assessment of broader Europe

<sup>2</sup> This paper only discusses the most recent vertical ground-motion models in Europe. The reader is referred to Bommer et al. (2011) for a detailed literature review on the entire progress of pan-European vertical GMPEs.



**Fig. 3** Horizontal (*top row*) and vertical (*bottom row*) DSF values of the proposed model as well as those of Rezaeian et al (2012; Retal12) and Eurocode 8 (CEN 2004) for  $M_w$  4.5 (*left panel*) and  $M_w$  7.5 (*right panel*) at  $R_{JB} = 10$  km for a rock site of  $V_{S30} = 800$  m/s



**Fig. 4** Effect of aleatory variability on horizontal and vertical DSF models proposed in this study

region for computing consistent horizontal and vertical pseudo-acceleration spectral ordinates for scenario-specific engineering studies. The presented V/H GMPE is also different from the model proposed by Ambraseys et al. (2005) as the latter developed an independent GMPE for the estimation of vertical spectral ordinates. The approach in Ambraseys et al. (2005) may produce vertical and horizontal spectral accelerations that are controlled by different

earthquake scenarios. As discussed briefly in introduction, different controlling earthquake scenarios for horizontal and vertical ground motions may cause practical difficulties in seismic design and performance assessment procedures that utilize compatible horizontal and vertical spectral demands. This shortcoming is prevailed by using V/H models as suggested in this paper. The particular features of the proposed V/H GMPE are described in the following paragraphs.

The proposed V/H model (Eq. 5) uses a functional form similar to that of Akkar et al. (2013a,b) horizontal GMPE for producing compatible vertical PSA as emphasized throughout the text. The magnitude scaling consists of a quadratic magnitude term as well as a hinging magnitude ( $c_1$ )—this is different than the coefficient defined in the DSF models—to account for magnitude saturation effects. The model considers magnitude dependency in geometrical spreading and describes the soil effects with a nonlinear site function that is based on  $V_{S30}$  and PGA at the reference rock site ( $V_{REF} = 750$  m/s). The effect of faulting mechanism on V/H is addressed by dummy variables  $F_N$  and  $F_R$  that are unity for normal and reverse faults, respectively, and zero otherwise.

$$\ln(V/H) = \begin{cases} a_1 + a_2(M_w - c_1) + a_3(8.5 - M_w)^2 + [a_4 + a_5(M_w - c_1)] \\ \ln\left(\sqrt{R_{JB}^2 + a_6^2}\right) + a_8 F_N + a_9 F_R + \ln(S) & \text{for } M_w \leq c_1 \\ a_1 + a_7(M_w - c_1) + a_3(8.5 - M_w)^2 + [a_4 + a_5(M_w - c_1)] \\ \ln\left(\sqrt{R_{JB}^2 + a_6^2}\right) + a_8 F_N + a_9 F_R + \ln(S) & \text{for } M_w > c_1 \end{cases} \quad (5a)$$

$$\ln(S) = \begin{cases} a_{10} \ln\left(\frac{V_{S30}}{V_{REF}}\right) - a_{11} \\ \ln\left[\frac{PGA_{REF} + c\left(\frac{V_{S30}}{V_{REF}}\right)^n}{(PGA_{REF} + c)\left(\frac{V_{S30}}{V_{REF}}\right)^n}\right] & \text{for } V_{S30} \leq V_{REF} \\ a_{10} \ln\left[\frac{\min(V_{S30}, 1000)}{V_{REF}}\right] & \text{for } V_{S30} > V_{REF} \end{cases} \quad (5b)$$

$$\ln(PGA_{REF}) = \begin{cases} \text{for } M_w \leq c_1 & 1.85329 + 0.0029(M_w - c_1) - 0.02807(8.5 - M_w)^2 \\ & + [-1.23452 + 0.2529(M_w - c_1)] \ln\left(\sqrt{R_{JB}^2 + 7.5^2}\right) - 0.1091 F_N + 0.0937 F_R \\ \text{for } M_w > c_1 & 1.85329 - 0.5096(M_w - c_1) - 0.02807(8.5 - M_w)^2 \\ & + [-1.23452 + 0.2529(M_w - c_1)] \ln\left(\sqrt{R_{JB}^2 + 7.5^2}\right) - 0.1091 F_N + 0.0937 F_R \end{cases} \quad (5c)$$

The regression coefficients  $a_1$  to  $a_{10}$  are computed from mixed-effects regression algorithm of Abrahamson and Youngs (1992). The magnitude and source-to-site distance measures are moment magnitude ( $M_w$ ) and Joyner–Boore distance ( $R_{JB}$ ) that are now almost standard in most of the predictive models in Europe. The hinging magnitude  $c_1$  is taken as 6.75 as in the case of Akkar et al. (2013a,b) horizontal GMPE after making several observations on the empirical data trend. The fictitious depth and the coefficients of linear magnitude terms ( $a_2$  and  $a_7$ ) are held fixed for the entire period range for a smooth spectral shape. The site amplification function, designated by  $\ln(S)$  in Eq. 5b, includes both linear and nonlinear soil amplification. The nonlinearity is considered by the reference horizontal peak ground acceleration ( $PGA_{REF}$ ) that is computed for  $V_{S30} = 750$  m/s (see Eq. 5c). The unit of  $PGA_{REF}$  is in terms of gravitational acceleration,  $g$ . The  $V_{S30}$  value of 750 m/s defines reference rock conditions in the V/H nonlinear site model, which is also the case in the nonlinear site

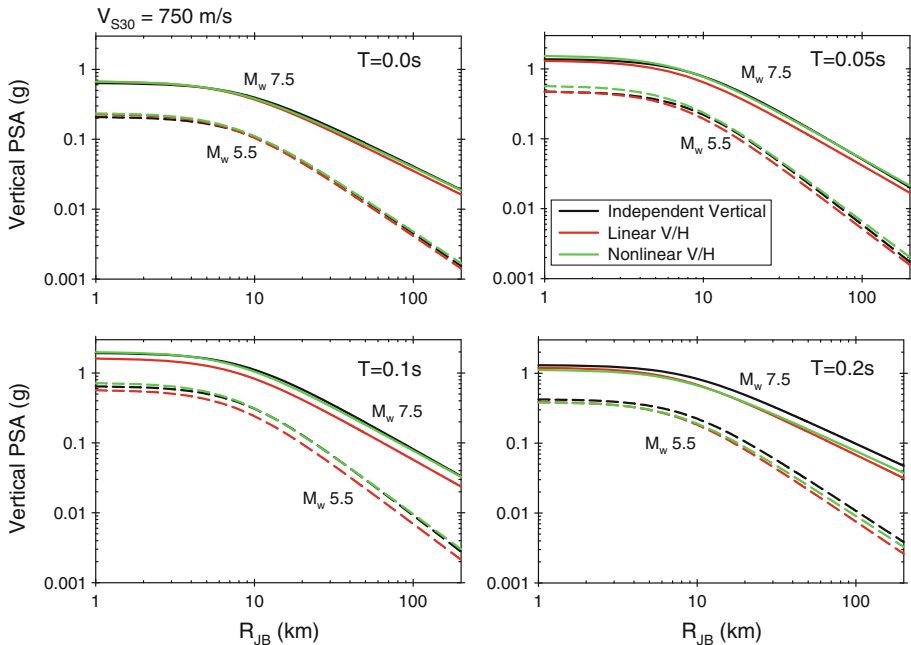
function of Akkar et al. (2013a,b) horizontal GMPE. The regression coefficients  $c$ ,  $n$ , and  $a_{11}$  are adopted from the Sandikkaya et al. (2013) site model.

## 5 Evaluation of proposed V/H GMPE with emphasis on nonlinear soil behavior

The nonlinear site behavior in the V/H model deserves some more discussion. The soil amplification of V/H inherently depends on the site behavior of vertical and horizontal acceleration components and it has yet to be better understood. In horizontal ground motions, the site-dependent amplification is represented by linear and nonlinear site terms. The latter term dominates at high ground-motion intensity levels and when  $V_{S30}$  attains low values (Choi and Stewart 2005; Walling et al. 2008; Sandikkaya et al. 2013). On the other hand, there is no clear evidence on the nonlinear site behavior of vertical ground motions. To our knowledge, the significance of nonlinearity in vertical ground motions has never been studied in detail from a GMPE perspective. Almost all independent vertical ground-motion GMPEs (e.g., Campbell and Bozorgnia 2003; Ambraseys et al. 2005; Cauzzi and Faccioli 2008) consider linear site behavior. Of the recently developed V/H GMPEs, Gülerce and Abrahamson (2011) account for nonlinear soil behavior whereas Bommer et al. (2011) disregard nonlinear site effects in V/H estimates.

From a theoretical view point, modeling nonlinear site effect for horizontal and vertical ground motions is always possible provided that the strong-motion metadata contains sufficient and reliable information on the modeling parameters. Observations on the empirical data trend as well as the significance of nonlinear term after regressions would define their potential impact in vertical and horizontal ground-motion estimates. The common assumption of log-normal distribution in horizontal and vertical ground motions imposes the same probability distribution for their ratio, which constitutes the basis of our logarithmic V/H model as given in Eq. (5a). Since site effects of horizontal and vertical ground motions are additive in the logarithmic V/H model, the contributions of linear and nonlinear site terms would control the overall V/H behavior and this should be mapped on to the estimated vertical ground motions.

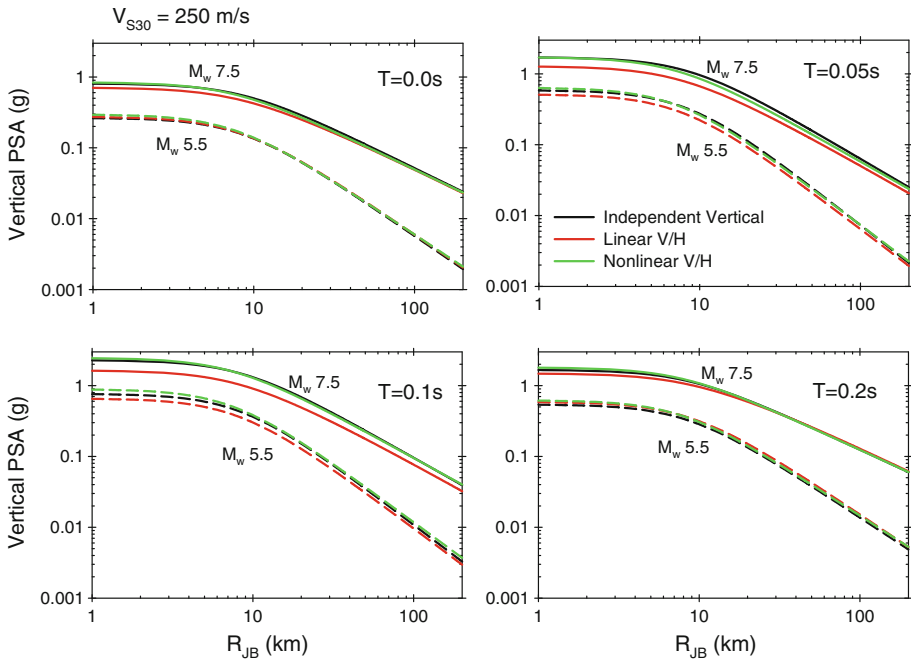
The above discussion is visually illustrated by Figs. 5 and 6 that show the median estimates of vertical PGA and PSA at  $T = 0.05, 0.1$  and  $0.2$  s. The vertical ground motions significantly affect the amplitudes of these high-frequency spectral ordinates as discussed in the previously cited references. The figures compare the median vertical ground-motion estimates of three alternative predictive models. The first predictive model is the one proposed in this study (designated as “Nonlinear V/H” on the figures). The second model constrains  $a_{11}$  to zero to disregard nonlinear site effects in Eq. (5b) and it is called as “Linear V/H” in Figs. 5 and 6. The last GMPE directly estimates the vertical spectral ordinates and it is defined as “Independent Vertical” on the plots. All three models are derived from the database used in this study. The third GMPE (independent vertical) disregards nonlinear site effects as neither the regression analysis nor the empirical data trends supported the effects of nonlinear soil behavior on vertical ground motions. Figure 5 shows the distance-dependent variation of median vertical ground-motion estimates from these alternative GMPEs for a generic rock site ( $V_{S30} = 750$  m/s) for  $M_w 7.5$  and  $M_w 5.5$ . The style-of-faulting is chosen as strike-slip for the scenario earthquakes. Figure 6 displays the same plots for a soft site represented by  $V_{S30} = 250$  m/s. The median horizontal spectral ordinates of the Akkar et al. (2013a,b) GMPE are modified by the linear and nonlinear V/H models to obtain the corresponding median vertical ground-motion estimates.



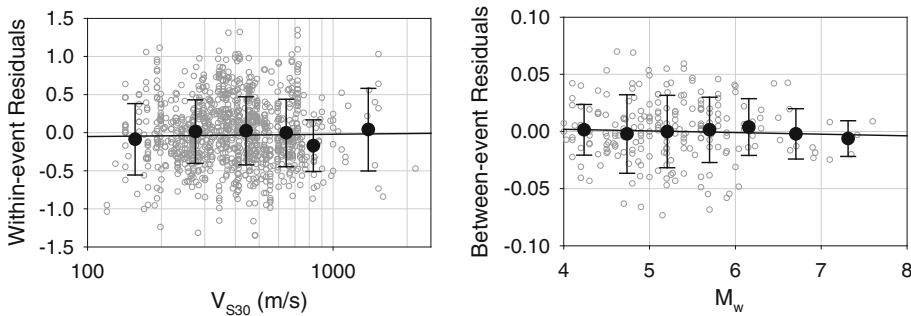
**Fig. 5** Median V/H estimates computed from linear and nonlinear V/H models as well as an independent vertical ground-motion GMPE. The chosen site represents generic rock conditions ( $V_{S30} = 750$  m/s). The comparisons are done for  $M_w$  7.5 (solid lines) and  $M_w$  5.5 (dashed lines) earthquakes generated by a strike-slip fault

The comparative plots in Fig. 5 indicate that all three GMPEs yield very similar vertical ground motions regardless of the variations in magnitude. The vertical ground-motion estimates from linear V/H model are slightly smaller with respect to the predictions of the other two GMPEs in many cases. The plots in Fig. 6 depict very similar vertical ground-motion estimates for nonlinear V/H and independent vertical GMPEs. The median plots almost overlap with each other for these models. The observed differences in linear V/H become more visible in Fig. 6. The observations from Figs. 5 and 6 suggest that the nonlinear site effects are not prominent in vertical ground motions regardless of the variations in magnitude and distance. Thus, independent vertical GMPEs may overlook nonlinear soil behavior. However, consideration of soil nonlinearity in V/H models provides a control over the nonlinear soil effects of horizontal ground motions. This approach results in mimicking the genuine variations in the vertical ground-motion demands when V/H ratios are implemented together with the horizontal GMPEs. Under the light of these discussions and because we prefer providing a V/H model instead of an independent vertical GMPE for consistency between horizontal and vertical earthquake scenarios, the site amplification function given in Eq. (5b) considers the nonlinear soil behavior.

The proposed model is also evaluated in terms of classical residual analysis. Figure 7 shows the within-event and between-event residuals for  $T = 0.2$  s. The within-event residuals (left panel) are plotted in terms of  $V_{S30}$  whereas between-event residuals (right panel) are plotted for moment magnitude,  $M_w$ . The plots also show the average residuals for a set of pre-determined  $V_{S30}$  and  $M_w$  intervals. The  $V_{S30}$  intervals have a uniform spacing of 180 m/s for  $V_{S30} \leq 900$  m/s. A single average of between-event residuals is computed for  $V_{S30} > 900$



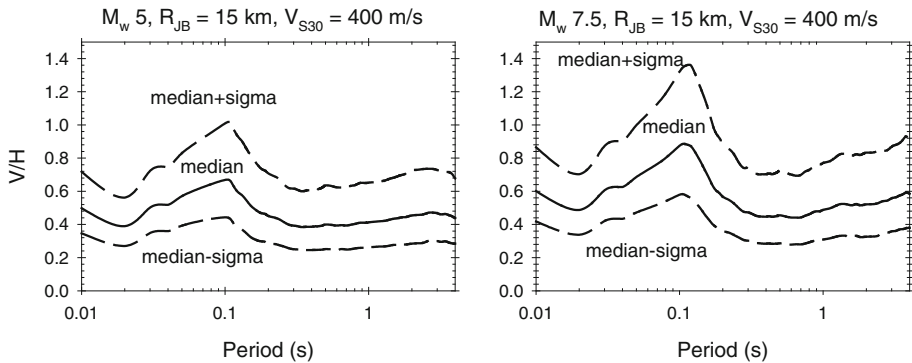
**Fig. 6** Median V/H estimates computed from linear and nonlinear V/H models as well as an independent vertical ground-motion GMPE. The chosen site represents generic rock conditions ( $V_{S30} = 250$  m/s). The comparisons are done for  $M_w 7.5$  (solid lines) and  $M_w 5.5$  (dashed lines) earthquakes generated by a strike-slip fault



**Fig. 7** Between- and within-event residual distributions for the V/H GMPE at  $T = 0.2$  s. The between-event residuals are plotted in terms of  $M_w$  whereas within-event residuals are given as a function of  $V_{S30}$

m/s as the data are sparse after this  $V_{S30}$  value. The  $M_w$  intervals are incremented by 0.5 units between  $4 \leq M_w \leq 7$ . The between-event residuals are also represented by a single average after  $M_w 7.0$  due to sparse data distribution. The residuals are randomly distributed over the magnitude and  $V_{S30}$  range considered in this study. Their averages for the pre-determined intervals fluctuate about zero. These observations suggest unbiased estimates of the proposed V/H GMPE. The random distribution of within-event residuals can be interpreted as the satisfactory performance of the preferred nonlinear site model. We produced similar residual plots for other spectral periods and the trends discussed for  $T = 0.2$  s are also valid for these figures. We did not show them in the paper for space considerations.





**Fig. 8** Effect of aleatory variability in the proposed V/H GMPE

Figure 8 shows the influence of aleatory variability on V/H estimates of the proposed model. The plots in Fig. 8 are prepared for earthquake scenarios of  $M_w$  5 (left panel) and  $M_w$  7.5 (right panel). The chosen  $V_{S30}$  value assumes stiff site conditions ( $V_{S30} = 400$  m/s). The fictitious site is at a distance of  $R_{JB} = 15$  km from strike-slip fault. The median  $\pm$  sigma curves indicate that the variations in vertical ground-motion amplitudes can be significant due to aleatory variability. This variation should be considered seriously in vector-valued probabilistic hazard studies. Table 5 lists the regression coefficients of the V/H GMPE for the same periods as of horizontal and vertical DSF models. The full list of regression coefficients for the entire spectral periods are given in the electronic supplementary to this article.

## 6 Details of the proposed V/H GMPE and its comparisons with the previous pan-European model

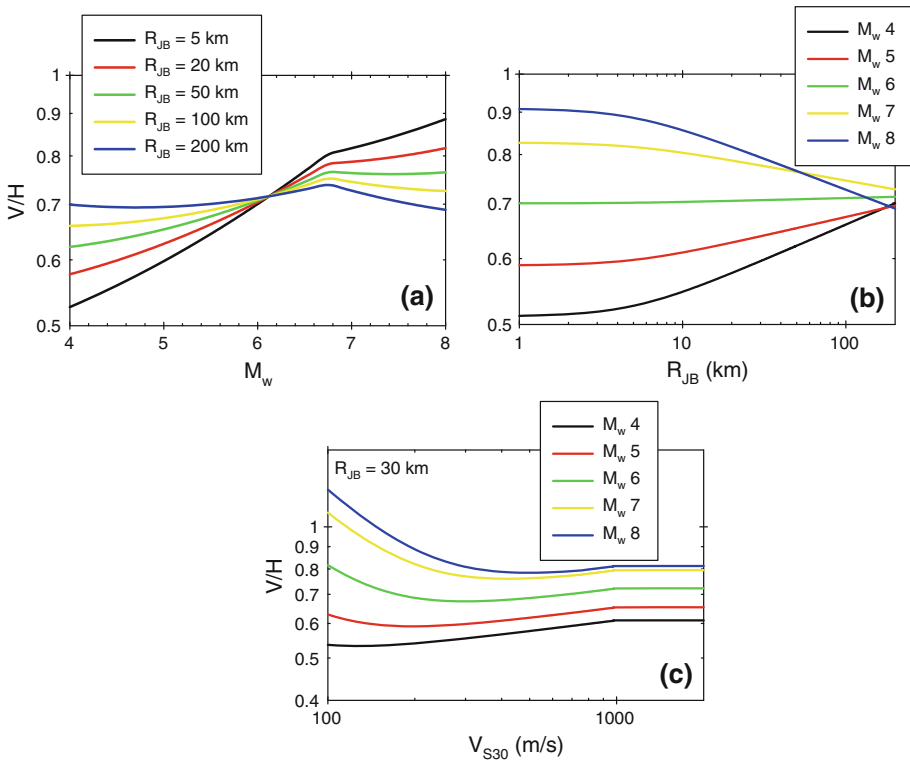
The proposed V/H model is studied further to have better insight about its behavior. Figure 9 shows the median V/H estimates for  $T = 0.1$  s under the variation of fundamental estimator parameters (i.e.,  $M_w$ ,  $R_{JB}$  and  $V_{S30}$ ). However, the discussions made here generally hold for the entire period range considered in this study. Figure 9a displays the magnitude-dependent V/H variation for different  $R_{JB}$  values. The assumed site condition is rock ( $V_{S30} = 750$  m/s) and the chosen SoF is strike-slip in this case. The median V/H curves indicate that for magnitudes up to  $M_w$  6 (acts like a node in this panel) one would expect larger V/H values with increasing distance. Thus, horizontal spectral ordinates tend to decay faster with respect to vertical spectral ordinates for small to moderate size events. This trend changes for  $M_w > 6$  and increase in distance yields a decrease in V/H ratios that eventually indicates slower decay of horizontal spectral ordinates with respect to their vertical counterparts. Fig. 9b that shows the distance-dependent behavior of V/H for a set of magnitude values supports the observations in Fig. 9a. The increase in distance yields larger V/H for magnitudes up to  $M_w$  6 that is reversed for  $M_w > 6$ . As pointed out in Fig. 9a, the horizontal spectral ordinates of small to moderate size events ( $M_w < 6$ ) attenuate faster with respect to their vertical counterparts and this trend reverses as magnitude becomes larger. The median V/H curve for  $M_w$  6 is almost insensitive to variations in distance, which explains its “nodal” position in Fig. 9a. Figure 9c that shows the particular influence of  $V_{S30}$  on V/H suggests that the vertical spectrum tends to attain larger values for soft to very soft sites ( $V_{S30} < 350$  m/s) and large magnitudes ( $M_w > 7$ ). As the site gets stiffer the variations in V/H are mild and stable.

**Table 5** Period-dependent regression coefficients of the V/H ground-motion model for the selected periods. Period-independent coefficients are given in the footnote\*

Period (s)	a <sub>1</sub>	a <sub>3</sub>	a <sub>4</sub>	a <sub>8</sub>	a <sub>9</sub>	a <sub>10</sub>	a <sub>11</sub>	φ**	τ**	σ**
PGA	-0.55429	0.03124	-0.01172	0.04174	0.00483	0.2153	-0.28846	0.3578	0.0663	0.3639
PGV	-0.83717	0.0253	0.06389	0.10829	0.10998	0.36054	-0.19688	0.3655	0.0204	0.3661
0.01	-0.54467	0.03109	-0.01347	0.04465	0.00688	0.20949	-0.28685	0.3571	0.0747	0.3648
0.02	-0.46655	0.03099	-0.02821	0.04626	0.00711	0.21464	-0.28241	0.3558	0.0844	0.3657
0.03	-0.25416	0.03095	-0.07133	0.04137	-0.00933	0.20684	-0.26842	0.3613	0.0969	0.3741
0.04	-0.03087	0.02804	-0.10768	0.02432	-0.06283	0.17531	-0.24759	0.373	0.1161	0.3907
0.05	0.09261	0.02211	-0.12033	-0.01097	-0.0786	0.11306	-0.22385	0.3922	0.1259	0.4119
0.075	-0.02755	0.01822	-0.07373	0.00883	-0.09063	0.06983	-0.17525	0.405	0.1377	0.4278
0.1	-0.2157	0.01558	-0.02512	0.01238	-0.15905	0.0824	-0.29293	0.4103	0.1701	0.4442
0.15	-0.79732	0.02578	0.06757	0.03577	-0.04592	0.15636	-0.39551	0.4455	0.1057	0.4579
0.2	-1.02981	0.03463	0.08653	0.05953	-0.00392	0.21837	-0.44644	0.4404	0.0816	0.4479
0.3	-1.14208	0.0382	0.09311	0.10302	0.05769	0.31643	-0.4573	0.4454	0.0249	0.4461
0.4	-1.09718	0.03975	0.09001	0.04878	0.07534	0.38181	-0.43008	0.4468	0.0828	0.4544
0.5	-1.0642	0.0401	0.08691	0.06349	0.09199	0.40009	-0.37408	0.4557	0.0674	0.4607
0.75	-0.89263	0.0349	0.0751	0.07806	0.10535	0.44592	-0.28957	0.4584	0.0256	0.4591
1	-0.73533	0.03063	0.0609	0.08829	0.11555	0.50958	-0.28702	0.4508	0.0252	0.4515
1.5	-0.70636	0.03203	0.0467	0.06958	0.12575	0.4262	-0.24695	0.4462	0.0864	0.4545
2	-0.62766	0.03247	0.0332	0.06344	0.13595	0.42834	-0.17336	0.4632	0.0518	0.4661
3	-0.42904	0.02433	0.0197	0.0934	0.14271	0.51101	-0.13336	0.4337	0.0686	0.4391
4	-0.35034	0.01392	0.00738	0.19948	0.15823	0.54615	-0.07749	0.4427	0.0821	0.4502

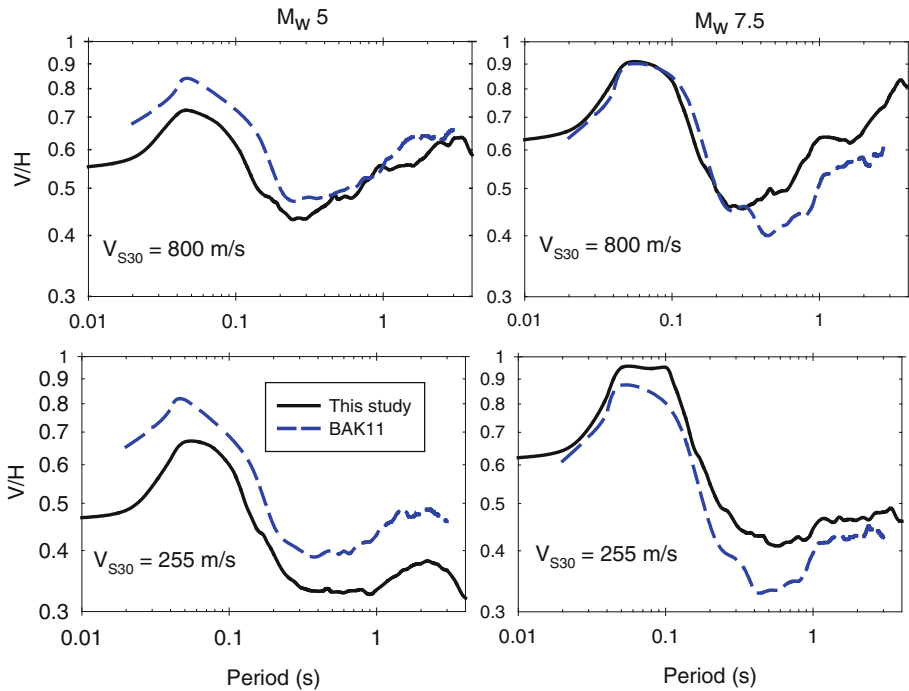
\*a<sub>2</sub> = 0.33; a<sub>5</sub> = -0.04; a<sub>6</sub> = 5; a<sub>7</sub> = 0.19; c<sub>1</sub> = 6.75; V<sub>REF</sub> = 750 m/s, c = 2.5; n = 3.2

\*\* φ, τ and σ refer to within-event, between-event and total standard deviations, respectively



**Fig. 9** Median V/H variations of the proposed model in terms major estimator parameters for  $T = 0.1$  s

The proposed model is also compared with the recent pan-European V/H GMPE that is developed by (Bommer et al. 2011; BAK11). The magnitude scaling is linear and geometrical spreading does not consider a magnitude dependent slope in BAK11. It disregards the soil nonlinearity in V/H estimates. Figure 10 compares the median V/H estimates of these two models. The comparisons are made for median V/H trends as this spectral quantity is used while constructing the horizontal spectrum compatible vertical spectral ordinates for scenario-specific PSHA. The details of this procedure are described in the subsequent sections. The spectral comparisons in Fig. 10 are done for  $R_{JB} = 10$  km for  $M_w 5$  and  $M_w 7.5$  (left and right columns, respectively). A strike-slip fault is used in the scenario earthquakes as in the case of previous examples. The top row panels compare the median V/H estimates for  $V_{S30} = 800$  m/s (generic rock site) whereas the bottom row comparisons are plotted for  $V_{S30} = 255$  m/s (soft soil). The median V/H estimates of the proposed model depict differences with respect to BAK11. However, the differences are not substantial. Our model tends to estimate larger V/H ratios towards longer periods for larger magnitudes. The opposite holds for small magnitudes and BAK11 yields larger V/H estimates particularly for softer sites. The discrepancies between the median V/H estimates of BAK11 and the proposed model can be the attributes of different functional forms as well as the size and resolution of databases although they are originated from the same region. This study uses a more complicated functional form that considers magnitude-dependent geometrical spreading as well as linear and nonlinear soil behavior as a function of continuous  $V_{S30}$ . These features are not included in BAK11 due to insufficient meta-

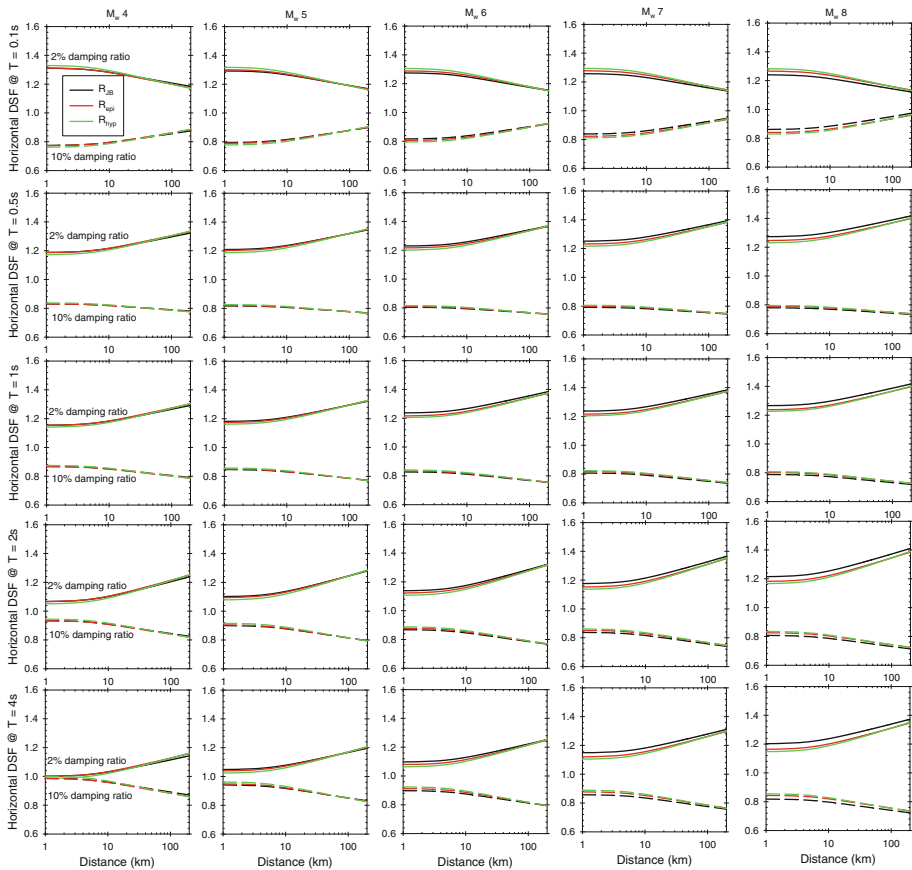


**Fig. 10** Comparison of the proposed equation with Bommer et al. (2011; BAK11) V/H model for different magnitudes and site conditions at  $R_{JB} = 10$  km

data features in their database. Although BAK11 and this study use strong-motion data collected from broader Europe, the pan-European database used in this study is recently updated and expanded in terms of waveform quality and metadata information (Akkar et al. 2013c).

## 7 Use of proposed DSF and V/H models for different point-source distance metrics

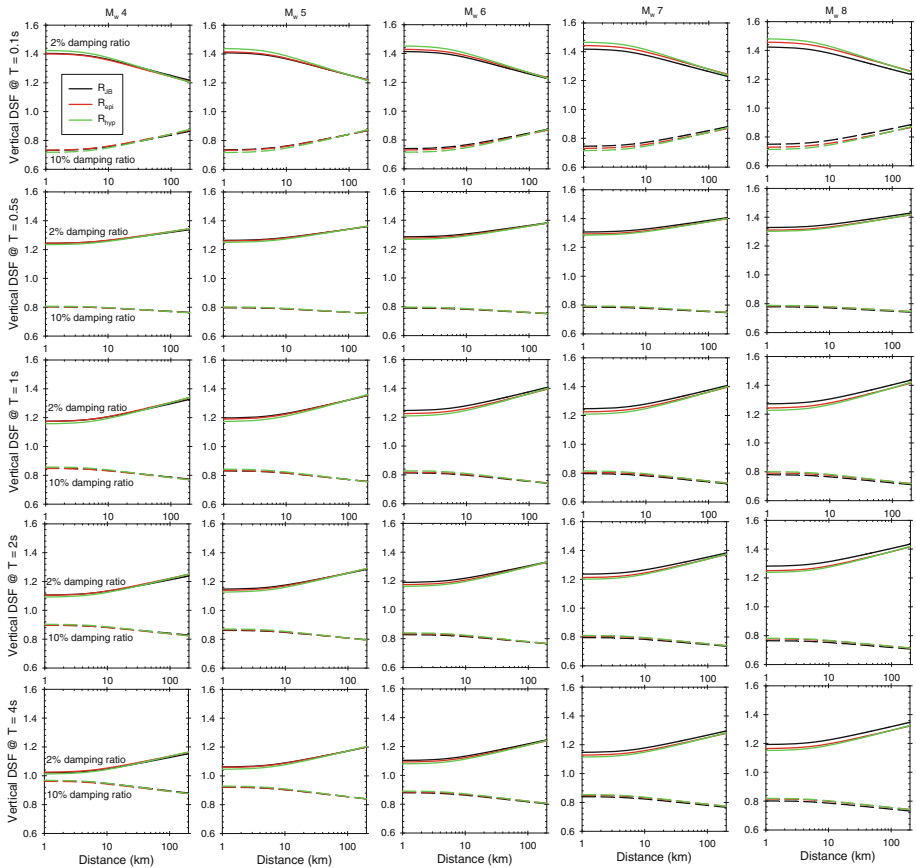
The proposed DSF and V/H GMPEs use  $R_{JB}$  as the source-to-site distance metric. This section provides information on the applicability of these models for point source distance measures (epicentral distance - $R_{epi}$ - and hypocentral distance - $R_{hyp}$ -) as Akkar et al. (2013a,b) GMPEs are developed for estimating horizontal ground motions in  $R_{epi}$ ,  $R_{hyp}$  and  $R_{JB}$ . Figure 11 shows median horizontal DSF estimates computed for  $R_{JB}$ ,  $R_{epi}$  and  $R_{hyp}$  for a stiff site of  $V_{S30} = 400$  m/s. The availability all three distance measures in our strong-motion database enabled us to develop DSF predictive GMPEs for the latter two distance measures. The same functional form as of  $R_{JB}$ -based DSF predictive model was used in these GMPEs and same steps were followed in the regressions. The distance range considered in comparisons is up to 200 km. Each row in Fig. 11 compares the median horizontal DSF estimates of  $R_{JB}$ ,  $R_{epi}$  and  $R_{hyp}$  for a specific period. The selected spectral periods for comparisons are  $T = 0.1$  s,  $T = 0.5$  s,  $T = 1.0$  s,  $T = 2.0$  s and  $T = 4.0$  s. They represent the overall spectral period interval of concern in the paper. Each column in Fig. 11 shows a specific magnitude taking values between  $M_w$  4 and  $M_w$  8 with unit increments. The comparisons are shown for 2 and



**Fig. 11** Comparisons of median horizontal DSF estimates from  $R_{JB}$ -,  $R_{epi}$ - and  $R_{hyp}$ -based GMPEs that are derived from the same strong-motion database. The functional forms of all three GMPEs are the same. The solid and dashed lines show the comparisons for 2 and 10% damping, respectively

10% damping ratios in order not to crowd the panels. The other damping ratios yield similar results to those given in Fig. 11. Figure 12 makes the same comparisons for vertical DSF estimates. The display format in this figure is the same as in Fig. 11. The comparative plots indicate that median horizontal and vertical DSF estimates are practically independent of distance definition. For lightly damped systems (represented by 2% critical damping in Figs. 11 and 12) and towards large magnitudes, the variations in  $R_{JB}$ -based DSF model are slightly different than the median DSF trends of the point-source distance metrics. However, the observed discrepancies are not more than 5% for the entire distance range. The observations highlighted by these plots are valid for the whole magnitude, period and damping ratios covered in this study. Thus, the overall discussions from Figs. 11 and 12 suggest the general applicability of  $R_{JB}$ -based horizontal and vertical DSF GMPEs for the modification of 5%-damped spectral ordinates of Akkar et al. (2013a,b) without making any adjustments for  $R_{epi}$  and  $R_{hyp}$ .

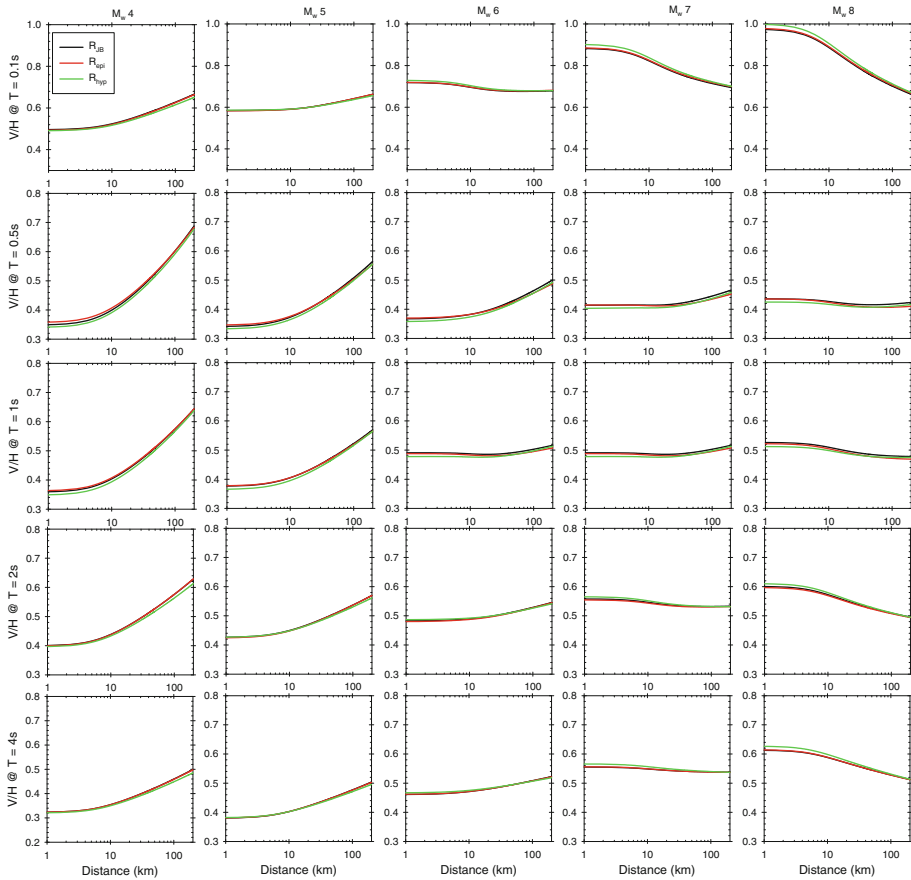
Similar comparisons are repeated for the median V/H estimates. Figure 13 shows the median V/H estimates of  $R_{JB}$ ,  $R_{epi}$  and  $R_{hyp}$  predictive models. The GMPEs for  $R_{epi}$  and  $R_{hyp}$  are developed by following the methodology described in the DSF comparisons: same



**Fig. 12** Comparisons of median vertical DSF estimates from  $R_{J_B}$ -,  $R_{epi}$ - and  $R_{hyp}$ -based GMPEs that are derived from the same strong-motion database. The functional forms of all three GMPEs are the same. The solid and dashed lines show the comparisons for 2 and 10% damping, respectively

functional forms as of  $R_{J_B}$ -based GMPE and same type of regression analysis by utilizing the strong-motion database used for developing  $R_{J_B}$ -based GMPE. The plots in Fig. 13 compare median V/H estimates for the above three distance measures by using the period and magnitude combinations given in Figs. 11 and 12. The comparisons in Fig. 13 display very similar patterns between the median V/H estimates of  $R_{epi}$ ,  $R_{hyp}$  and  $R_{J_B}$  GMPEs. Although some minor discrepancies in V/H trends do exist between  $R_{hyp}$  and the other two distance metrics, we believe that these differences can be neglected for all practical purposes. Thus, one can use our  $R_{J_B}$ -based V/H model in confidence with the Akkar et al. (2013a,b) horizontal GMPEs of all three distance measures to generate fully consistent vertical ground-motion estimates.

The conclusions derived from the median DSF and V/H comparisons are further investigated by studying the total standard deviations of the DSF and V/H GMPEs that are developed separately for each source-to-site distance metric. The comparative results are shown in Fig. 14. The left and right panels in the first row of Fig. 14 show the period-dependent variation of total sigma for horizontal and vertical DSF GMPEs. The panel in the second row displays same type of comparisons for V/H model. The information inferred from Fig. 14 once again

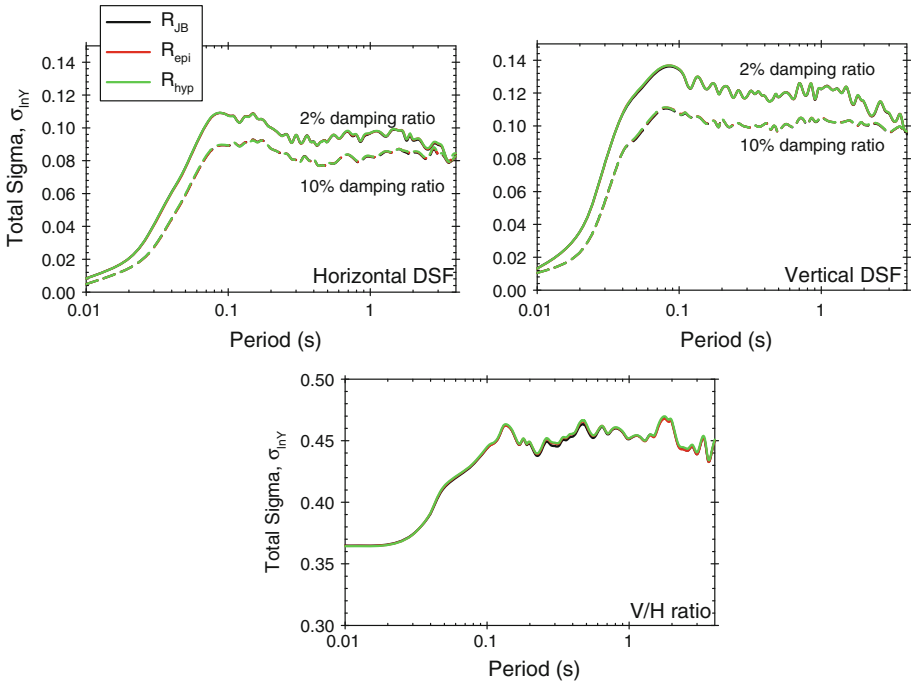


**Fig. 13** Comparisons of median V/H estimates from  $R_{JB}$ -,  $R_{epi}$ - and  $R_{hyp}$ -based GMPEs that are developed from the same database. The functional forms of the predictive models are the same

justifies that any existing difference among the three considered distance measures becomes immaterial for DSF and V/H ratio estimates.

### 8 Developing consistent scenario-based horizontal and vertical pseudo-acceleration spectra

The use of V/H GMPEs together with conditional mean spectrum (CMS; Baker 2011) yields consistent scenario-based horizontal and vertical design spectra (Gülerce and Abrahamson 2011). CMS has the ability of representing more realistic scenario-based horizontal seismic demands as it accounts for the correlation of ground-motion variability at different spectral periods. When V/H model is considered together with CMS, the proper handling of horizontal and vertical ground-motion variability would yield a vertical spectrum that represents consistent vertical seismic demands with the horizontal earthquake scenario. The consistent horizontal and vertical spectra will essentially lead to more realistic selection and scaling of horizontal and vertical ground motions for a specific target earthquake scenario.



**Fig. 14** Comparison of total standard deviations of DSF (*top row*) and V/H (*bottom row*) GMPEs developed for different distance measures

The proposed V/H model is compatible with the Akkar et al. (2013a,b) GMPE derived for horizontal PSA as both studies used exactly the same ground-motion database. Thus, both GMPEs can be employed together for the calculation of consistent CMS for horizontal and vertical ground motions. The complete form of consistent horizontal and vertical CMS is given in Eq. (6) (Baker 2011; Gülerce and Abrahamson 2011).

$$CMS_H(T_0, T) = \mu_H(T) \cdot \exp(\rho_H(T_0, T) \varepsilon(T_0) \sigma_H(T)) \tag{6a}$$

$$CMS_V(T_0, T) = CMS_H(T_0, T) \cdot \mu_{V/H}(T) \cdot \exp(\rho_{H,V/H}(T_0, T) \cdot \sigma_{V/H}(T)) \tag{6b}$$

In the above expressions  $\mu_H(T)$  is the median estimates of the horizontal GMPE for the most contributing earthquake scenario identified after deaggregation analysis for the reference period  $T_0$ . The parameter  $\sigma_H(T)$  is the total standard deviation of the horizontal GMPE.  $\varepsilon(T_0)$  is the number of standard deviations between the target spectral ordinate at  $T_0$  and median ground-motion estimation at the same period for the most contributing earthquake scenario. The correlation coefficient between epsilons at spectral period  $T$  and  $T_0$  is defined by  $\rho_H(T_0, T)$ . Table 6 gives the correlation coefficient matrix,  $\rho_H(T_0, T)$ , for the selected spectral periods using the Akkar et al. (2013a,b) horizontal GMPE. The entire correlation coefficient matrix for the whole set of spectral periods is given in the electronic supplement.

The simplified vertical CMS,  $CMS_V(T_0, T)$ , is computed by multiplying the median V/H,  $\mu_{V/H}(T)$ , with the horizontal CMS. Note that  $\mu_{V/H}(T)$  should represent the most contributing horizontal earthquake scenario for internal consistency with the horizontal CMS. These are the first two terms in Eq. (6b). The fully consistent vertical CMS with the horizontal earthquake scenario requires the consideration of ground-motion variability between the horizontal and vertical components that is given as the third multiplicative term in Eq. (6b).



**Table 6** Period-dependent correlation coefficient matrix of  $\rho_H(T_0, T)$

Period (s)	PGA	0.01	0.02	0.03	0.04	0.05	0.075	0.1	0.15	0.2	0.3	0.4	0.5	0.75	1	1.5	2	3	4
PGA	1	0.99966	0.99784	0.99198	0.98153	0.96686	0.93427	0.93426	0.91839	0.89789	0.834	0.77764	0.72497	0.62005	0.54546	0.47169	0.46411	0.41179	0.32908
0.01		1	0.99846	0.99296	0.98254	0.96805	0.93589	0.93534	0.91889	0.89695	0.83133	0.77413	0.72114	0.61654	0.54163	0.46768	0.46038	0.40905	0.32759
0.02			1	0.99608	0.98639	0.97227	0.9372	0.93377	0.91548	0.8903	0.82278	0.76584	0.7126	0.61209	0.53828	0.46527	0.45893	0.40769	0.32748
0.03				1	0.99265	0.98009	0.9412	0.9326	0.90798	0.87569	0.7996	0.74114	0.68874	0.59241	0.52024	0.45063	0.44787	0.39706	0.31963
0.04					1	0.99187	0.95046	0.93156	0.89437	0.85412	0.76727	0.70701	0.65557	0.56179	0.49043	0.42901	0.43238	0.38185	0.30985
0.05						1	0.96226	0.93485	0.88309	0.83332	0.73418	0.67099	0.61977	0.52614	0.4561	0.40005	0.40762	0.35783	0.28706
0.075							1	0.96262	0.88845	0.82352	0.70328	0.62602	0.56314	0.45335	0.38092	0.32316	0.3293	0.29077	0.24481
0.1								1	0.9362	0.86357	0.72956	0.64721	0.5722	0.45198	0.37881	0.31776	0.32079	0.28606	0.24612
0.15									1	0.9324	0.78904	0.69128	0.60976	0.47406	0.38947	0.3097	0.30067	0.26877	0.23962
0.2										1	0.88286	0.78939	0.70903	0.56265	0.47235	0.37342	0.35455	0.32109	0.26723
0.3											1	0.92243	0.8407	0.69909	0.60728	0.48496	0.4531	0.40003	0.30679
0.4												1	0.93712	0.79936	0.7063	0.57523	0.5291	0.46726	0.35461
0.5													1	0.88239	0.79308	0.66474	0.61543	0.54678	0.42548
0.75														1	0.92838	0.80638	0.74174	0.64541	0.53024
1															1	0.90458	0.84345	0.75232	0.63531
1.5																1	0.9411	0.85455	0.73478
2																	1	0.91408	0.79894
3																		1	0.93102
4																			1

This exponential term consists of the total standard deviation of V/H model and the correlation between the epsilons of horizontal and V/H GMPEs. The total standard deviation is composed of within- and between-event standard deviations. Thus, the correlation between the epsilons of horizontal and V/H GMPEs requires separate consideration of within- and between-event epsilon correlations of horizontal and V/H models. This is given in Eq. (7).

$$\rho_{H,V/H}(T_H, T_{V/H}) = \frac{\phi_H(T_H)\phi_{V/H}(T_{V/H})\rho_{H,V/H}^\phi(T_H, T_{V/H}) + \tau_H(T_H)\tau_{V/H}(T_{V/H})\rho_{H,V/H}^\tau(T_H, T_{V/H})}{\sigma_H(T_H)\sigma_{V/H}(T_{V/H})} \quad (7)$$

The within-event standard deviations of horizontal and V/H GMPEs are designated as  $\phi_H$  and  $\phi_{V/H}$  in Eq. (7), respectively. Similarly,  $\tau_H$  and  $\tau_{V/H}$  stand for the between-event standard deviations of horizontal and V/H GMPEs, respectively. The parameters  $\rho_{H,V/H}^\phi$  and  $\rho_{H,V/H}^\tau$  indicate the within- and between-event correlations between the horizontal and V/H GMPEs. Tables 7 and 8 list the within- and between-event correlation coefficient matrices by considering the proposed V/H model and the Akkar et al. (2013a,b) horizontal GMPE. The negative correlations in Tables 7 and 8 indicate an inverse relationship between the expected values of horizontal spectral ordinates and V/H ratios. The full list of within- and between-event correlation coefficient matrices for the whole spectral periods are given in the electronic supplementary to this article.

## 9 Summary and conclusions

This paper presents ground-motion models to estimate horizontal and vertical damping scaling factors and vertical-to-horizontal PSA ratios by using a subset of the most recent pan-European strong-motion databank that is assembled within the context of SHARE and SIGMA projects (RESORCE; Akkar et al. 2013c). The spectral period range of the GMPEs is between 0.01 and 4.0s. The V/H GMPE additionally estimates horizontal-to-vertical PGA and PGV ratios. The proposed models use the same subset of RESORCE as of Akkar et al. (2013a,b) GMPE that is developed for estimating the 5%-damped horizontal PSA. Thus, the GMPEs presented in this paper complement Akkar et al. (2013a,b) predictive model for its modification for consistent vertical design spectrum as well as horizontal and vertical spectral ordinates of damping ratios other than 5%. Although they are derived for  $R_{JB}$ , our verifications showed that these models are equally applicable to Akkar et al. (2013a,b) horizontal ground-motion estimates that are based on  $R_{epi}$  and  $R_{hyp}$ . The presented models as well as the Akkar et al. (2013a,b) horizontal GMPE, when used together, can serve for consistent vector-valued PSHA in the broader Europe region.

The horizontal and vertical damping scaling models use  $M_w$ ,  $R_{JB}$  and  $V_{S30}$  as independent parameters and can modify 5%-damped spectral ordinates for damping levels ranging between 1 and 50%. They are applicable of moment magnitudes between 4 and 8 and for distances up to 200 km. These models can also serve for the future updates of damping scaling factors in Eurocode 8 (CEN 2004) as the comparisons given in the paper indicate biased spectrum estimates of Eurocode 8 for very short periods and high damping ratios.

The proposed V/H GMPE considers  $M_w$ ,  $R_{JB}$ , SoF and  $V_{S30}$ -based nonlinear site function. The recommended magnitude and distance ranges of the predictive model are the same as those of damping scaling GMPEs. The nonlinear site model has an applicability range of  $150 \text{ m/s} \leq V_{S30} \leq 1200 \text{ m/s}$ . As the model is compatible with the Akkar et al. (2013a,b)

**Table 7** Period-dependent correlation coefficient matrix for  $\rho_{H,V,H}^{\phi}$

Period (s)*	PGA	0.01	0.02	0.03	0.04	0.05	0.075	0.1	0.15	0.2	0.3	0.4	0.5	0.75	1	1.5	2	3	4
PGA	-0.4091	-0.4072	-0.3919	-0.3565	-0.3371	-0.375	-0.316	-0.35	-0.3477	-0.3394	-0.2969	-0.3017	-0.2317	-0.2216	-0.1481	-0.1093	-0.1197	-0.1048	-0.1565
0.01	-0.4083	-0.4074	-0.3921	-0.357	-0.338	-0.3754	-0.3172	-0.3502	-0.3484	-0.3395	-0.2958	-0.2995	-0.2301	-0.2222	-0.1479	-0.1081	-0.1192	-0.1046	-0.1565
0.02	-0.4035	-0.4028	-0.3895	-0.354	-0.3365	-0.3749	-0.3181	-0.3487	-0.3485	-0.3395	-0.2943	-0.2933	-0.2255	-0.2228	-0.1489	-0.1104	-0.1222	-0.1077	-0.1585
0.03	-0.3936	-0.3936	-0.3778	-0.3432	-0.3274	-0.3768	-0.3258	-0.356	-0.3485	-0.336	-0.2849	-0.276	-0.2091	-0.207	-0.1392	-0.1066	-0.1204	-0.1065	-0.1559
0.04	-0.3757	-0.3757	-0.3575	-0.3172	-0.3174	-0.3768	-0.3302	-0.3566	-0.3377	-0.3197	-0.2645	-0.2539	-0.1892	-0.1894	-0.1178	-0.1021	-0.1196	-0.1042	-0.1595
0.05	-0.3571	-0.3563	-0.336	-0.2905	-0.2885	-0.3713	-0.3385	-0.3633	-0.339	-0.3215	-0.2576	-0.2403	-0.173	-0.1723	-0.1023	-0.0898	-0.1121	-0.0932	-0.1447
0.075	-0.337	-0.338	-0.318	-0.273	-0.2454	-0.302	-0.3731	-0.3818	-0.3591	-0.3402	-0.2465	-0.2311	-0.1476	-0.1544	-0.0935	-0.057	-0.0767	-0.0621	-0.1177
0.1	-0.3421	-0.3417	-0.3221	-0.286	-0.2591	-0.3023	-0.3095	-0.4159	-0.3978	-0.3512	-0.2378	-0.2327	-0.1466	-0.1416	-0.0764	-0.0418	-0.0591	-0.0416	-0.1013
0.15	-0.3469	-0.344	-0.3306	-0.2963	-0.2655	-0.2952	-0.2542	-0.3283	-0.443	-0.397	-0.2679	-0.2412	-0.1665	-0.168	-0.0969	-0.0357	-0.0307	0.00068	-0.0805
0.2	-0.3593	-0.357	-0.3502	-0.3245	-0.3005	-0.3008	-0.2214	-0.2741	-0.3304	-0.4301	-0.3226	-0.3155	-0.2351	-0.2207	-0.161	-0.0851	-0.0768	-0.048	-0.1101
0.3	-0.3092	-0.3062	-0.307	-0.3097	-0.2846	-0.2438	-0.1493	-0.1705	-0.1756	-0.252	-0.4155	-0.3952	-0.3078	-0.272	-0.1978	-0.1237	-0.1297	-0.1071	-0.1624
0.4	-0.2735	-0.2711	-0.2748	-0.2916	-0.2687	-0.2295	-0.1096	-0.1155	-0.1192	-0.1668	-0.2999	-0.4388	-0.3387	-0.3049	-0.2165	-0.1584	-0.1518	-0.1471	-0.168
0.5	-0.2424	-0.2408	-0.2456	-0.2701	-0.2515	-0.2104	-0.0833	-0.0734	-0.0735	-0.122	-0.2107	-0.3269	-0.3474	-0.3143	-0.2396	-0.1834	-0.1806	-0.1981	-0.2159
0.75	-0.1654	-0.1621	-0.1704	-0.2002	-0.1943	-0.1575	-0.0499	-0.0119	0.01827	-0.0234	-0.1208	-0.1857	-0.1816	-0.3316	-0.2653	-0.2413	-0.2204	-0.2285	-0.2726
1	-0.1261	-0.1227	-0.1334	-0.164	-0.1599	-0.1209	-0.019	-0.0068	0.05126	0.01853	-0.0806	-0.1171	-0.0947	-0.2038	-0.2754	-0.2587	-0.2459	-0.2509	-0.296
1.5	-0.0567	-0.0523	-0.0613	-0.0854	-0.0935	-0.0725	0.02833	0.03924	0.09688	0.0774	-0.0406	-0.0756	-0.0348	-0.0653	-0.0928	-0.2818	-0.2705	-0.2933	-0.3369
2	-0.0545	-0.046	-0.051	-0.0714	-0.0838	-0.0696	0.02018	0.02176	0.08436	0.07474	-0.0513	-0.0764	-0.0421	-0.0465	-0.0397	-0.1758	-0.2967	-0.3127	-0.3511
3	-0.0222	-0.019	-0.0202	-0.0413	-0.0532	-0.0374	0.05473	0.03042	0.08832	0.06402	-0.039	-0.0819	-0.0569	-0.0269	-0.0113	-0.0823	-0.1463	-0.378	-0.4341
4	-0.008	-0.0067	-0.0109	-0.0292	-0.0419	0.00535	0.0713	0.0468	0.08125	0.03232	-0.0738	-0.0826	-0.0546	-0.0172	-0.0313	-0.0691	-0.1195	-0.336	-0.4955

\* Periods in the first column are for the horizontal GMPE whereas the periods in the first row belong to the V/H model

**Table 8** Period-dependent correlation coefficient matrix for  $\rho_{H, V/H}^*$

Period (s)*	PGA	0.01	0.02	0.03	0.04	0.05	0.075	0.1	0.15	0.2	0.3	0.4	0.5	0.75	1	1.5	2	3	4
PGA	-0.3738	-0.3634	-0.3513	-0.3224	-0.2497	-0.2078	-0.2567	-0.3224	-0.3145	-0.3221	-0.2549	-0.2151	-0.1752	-0.1989	-0.1862	-0.0807	-0.0324	-0.0195	-0.0456
0.01	-0.3732	-0.3638	-0.352	-0.3231	-0.25	-0.2083	-0.2562	-0.3234	-0.3153	-0.3217	-0.2543	-0.215	-0.1751	-0.2004	-0.1874	-0.0799	-0.0333	-0.019	-0.0462
0.02	-0.3726	-0.3627	-0.3523	-0.3226	-0.2545	-0.2184	-0.2661	-0.3325	-0.3181	-0.3183	-0.245	-0.2023	-0.1612	-0.19	-0.1792	-0.0796	-0.0313	-0.0203	-0.0393
0.03	-0.3645	-0.3536	-0.3427	-0.3119	-0.2505	-0.2267	-0.273	-0.3462	-0.324	-0.3233	-0.2428	-0.1877	-0.1473	-0.1826	-0.1711	-0.0838	-0.0349	-0.0215	-0.0312
0.04	-0.3493	-0.339	-0.3265	-0.289	-0.2361	-0.23	-0.2844	-0.3576	-0.3297	-0.3237	-0.2254	-0.165	-0.1296	-0.1753	-0.1584	-0.0967	-0.0505	-0.0276	-0.0202
0.05	-0.3255	-0.3153	-0.3041	-0.2634	-0.2114	-0.218	-0.2797	-0.359	-0.3381	-0.3343	-0.225	-0.1471	-0.1182	-0.1804	-0.1452	-0.0928	-0.0497	-0.0286	-0.0187
0.075	-0.3035	-0.2991	-0.2878	-0.2525	-0.1781	-0.1519	-0.2811	-0.371	-0.3455	-0.3482	-0.2359	-0.1456	-0.1176	-0.1813	-0.1415	-0.0648	-0.0349	-0.0016	-0.0164
0.1	-0.3379	-0.332	-0.3243	-0.2923	-0.2101	-0.1686	-0.2594	-0.3918	-0.374	-0.3576	-0.2455	-0.1575	-0.124	-0.1734	-0.1416	-0.044	-0.0242	0.02349	-0.0347
0.15	-0.3338	-0.323	-0.3183	-0.2885	-0.2086	-0.1652	-0.2029	-0.3046	-0.3959	-0.3697	-0.2437	-0.1893	-0.1213	-0.1583	-0.1609	-0.0456	-0.0237	0.03357	-0.0224
0.2	-0.3325	-0.3239	-0.3153	-0.296	-0.2068	-0.1326	-0.1583	-0.2262	-0.3153	-0.3778	-0.2872	-0.275	-0.1934	-0.1913	-0.2256	-0.0894	-0.0497	-0.0093	-0.0511
0.3	-0.2837	-0.2748	-0.2672	-0.261	-0.169	-0.0544	-0.0836	-0.0925	-0.1458	-0.1832	-0.3141	-0.3606	-0.2722	-0.2377	-0.2564	-0.115	-0.0809	-0.0538	-0.1106
0.4	-0.2579	-0.251	-0.2456	-0.2298	-0.1478	-0.048	-0.0611	-0.0353	-0.1015	-0.1676	-0.251	-0.3956	-0.2842	-0.2737	-0.2442	-0.1293	-0.0988	-0.0873	-0.1128
0.5	-0.2338	-0.2276	-0.2202	-0.2096	-0.1325	-0.0406	-0.0488	-0.0146	-0.045	-0.1196	-0.1753	-0.3377	-0.2987	-0.2742	-0.2318	-0.1316	-0.121	-0.1311	-0.1269
0.75	-0.2004	-0.1943	-0.1876	-0.1746	-0.113	-0.0435	-0.0454	-0.0028	0.01116	-0.0551	-0.0715	-0.1907	-0.1583	-0.2623	-0.1718	-0.1132	-0.127	-0.1277	-0.1176
1	-0.2026	-0.1965	-0.1871	-0.1821	-0.1282	-0.0492	-0.0555	-0.029	0.027	-0.0297	-0.0208	-0.1259	-0.1051	-0.1578	-0.1491	-0.0999	-0.0898	-0.1428	-0.0907
1.5	-0.1856	-0.1766	-0.1677	-0.1599	-0.1229	-0.0632	-0.0479	-0.0541	0.05525	-0.0075	0.02422	-0.0554	-0.0249	-0.0106	0.02375	-0.0614	-0.0238	-0.1382	-0.053
2	-0.1887	-0.1792	-0.1669	-0.1648	-0.1302	-0.0758	-0.0518	-0.0821	0.046	-0.0023	0.03096	-0.0187	-0.0195	0.03288	0.04779	0.01938	-0.0428	-0.1261	-0.0188
3	-0.1625	-0.1601	-0.1538	-0.1547	-0.1155	-0.0687	-0.0383	-0.0911	0.04182	-0.0298	0.04972	0.02461	0.02969	0.09063	0.07666	0.09121	0.0573	-0.1434	-0.0449
4	-0.0832	-0.086	-0.0924	-0.1004	-0.0845	-0.0414	0.06344	-0.0056	0.04267	0.00134	0.07722	0.02463	0.06808	0.14908	0.14995	0.20841	0.08965	-0.0882	-0.178

\* Periods in the first column are for the horizontal GMPE whereas the periods in the first row belong to the V/H model

horizontal GMPE we present epsilon-based correlation coefficients for deriving consistent horizontal and vertical CMS for scenario-based hazard studies in Europe and surrounding regions. The V/H model can also be used for future updates of vertical seismic demands in Eurocode 8 (CEN 2004).

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