Name and Surname: Student Number:

Math 466 - Fall 2019 - METU

## Quiz 7

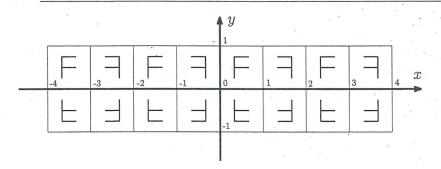
Consider the following isometries. There are eleven of them.

• 
$$\alpha_k(x,y) = (x+k,y)$$
 for  $k=1,2,3,4$ .

• 
$$\beta_k(x,y) = (x+k,-y)$$
 for  $k = 1, 2, 3, 4$ .

• 
$$\gamma_1(x,y) = (-x,y), \gamma_2(x,y) = (x,-y), \text{ and } \gamma_3(x,y) = (-x,-y).$$

For each of the following frieze patterns, let G be the group of isometries fixing that pattern.

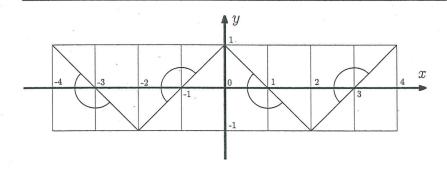


1. Cross out the isometries which are not suitable:

$$\{\alpha_1, \alpha_2, \alpha_3, \alpha_4, \beta_4, \beta_2, \beta_3, \beta_4, \gamma_1, \gamma_2, \gamma_3\} \subset G.$$

2. Determine the groups H and J.

$$H = \langle \alpha_2 \rangle$$
  
 $J = \{id, \delta_1, \delta_2, \delta_3 \}$ 



1. Cross out the isometries which are not suitable:

$$\{\mathscr{A}_{1}, \mathscr{A}_{2}, \mathscr{A}_{8}, \alpha_{4}, \mathscr{A}_{1}, \mathscr{A}_{2}, \mathscr{B}_{2}, \mathscr{B}_{8}, \mathscr{B}_{4}, \mathscr{A}_{1}, \mathscr{A}_{8}, \mathscr{B}_{8}\} \subset G.$$

2. Determine the groups H and J.