

### EXAMPLE 3.2

ORIGIN := 1

$T := 340$        $P := 30$        $R := 83.14$        $T_c := 190.6$        $P_c := 46.1$        $\omega := 0.011$

$$T_r := \frac{T}{T_c} \quad P_r := \frac{P}{P_c}$$

$$\alpha := \left[ 1 + \left( 0.37464 + 1.54226 \cdot \omega - 0.26992 \cdot \omega^2 \right) \cdot \left( 1 - \sqrt{T_r} \right) \right]^2$$

$$A := 0.45724 \cdot \left( \frac{P_r}{T_r^2} \right) \cdot \alpha \quad B := 0.0778 \cdot \frac{P_r}{T_r}$$

$$p := -1 + B \quad q := A - 2 \cdot B - 3 \cdot B^2 \quad r := -A \cdot B + B^2 + B^3$$

$$M := Z^3 + p \cdot Z^2 + q \cdot Z + r = 0 \quad \left\{ \begin{array}{l} \text{solve} \\ \text{assume, } Z = \text{real} \end{array} \right. \rightarrow 0.96106207724021429375$$

$$Z := \max(M) = 0.961$$

$$V := \frac{Z \cdot R \cdot T}{P} = 905.564$$

### Alternative Approach

$$\text{root}(p, q, r) := \left| \begin{array}{l} v \leftarrow \begin{pmatrix} r \\ q \\ p \\ 1 \end{pmatrix} \\ x \leftarrow \text{polyroots}(v) \\ \text{for } i \in 1 \dots 3 \\ \quad x_i \leftarrow 0 \text{ if } \text{Im}(x_i) \neq 0 \\ x1 \leftarrow \max(x) \\ y \leftarrow \min(x) \\ x2 \leftarrow \begin{cases} \max(x) & \text{if } y = 0 \\ y & \text{otherwise} \end{cases} \\ \begin{pmatrix} x1 \\ x2 \end{pmatrix} \end{array} \right.$$

$$\underline{Z} := \text{root}(p, q, r) = \begin{pmatrix} 0.961 \\ 0.961 \end{pmatrix}$$

$$\underline{V}(T, P) := \left| \begin{array}{l} T_r \leftarrow \frac{T}{T_c} \\ P_r \leftarrow \frac{P}{P_c} \\ \alpha \leftarrow \left[ 1 + (0.37464 + 1.54226 \cdot \omega - 0.26992 \cdot \omega^2) \cdot (1 - \sqrt{T_r}) \right]^2 \\ A \leftarrow 0.45724 \cdot \left( \frac{P_r}{T_r^2} \right) \cdot \alpha \\ B \leftarrow 0.0778 \cdot \frac{P_r}{T_r} \\ p \leftarrow -1 + B \\ q \leftarrow A - 2 \cdot B - 3 \cdot B^2 \\ r \leftarrow -A \cdot B + B^2 + B^3 \\ Z \leftarrow \text{root}(p, q, r)_1 \\ V \leftarrow \frac{Z \cdot R \cdot T}{P} \\ V \end{array} \right.$$

$$V(340, 30) = 905.564$$